CISC 2210 Spring 2018 Quiz 2

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1 Basic Logic (3 points)

Let:

 $\mathcal{O}=$ "3 is an odd number."

E = "4 is an even number."

 $P="\pi$ is a rational number."

 $\mathbf{Q} = "\pi = \mathbf{q} \text{ for some } q \in \mathbb{Q}."$

Express the following in logical notation:

- 1. 3 is an even number or 4 is an even number.
- 2. π is an irrational number.
- 3. If π is a rational number, then $\pi=q$ for some $q\in\mathbb{Q}.$

2 Truth tables (2 points)

Create a truth table for $(P \lor Q) \to R$

3 Logic Proofs (5 points)

1. Prove that $(\neg Q \land (P \rightarrow Q)) \rightarrow \neg P$ is tautological. (2 points)

2. Prove that $\neg(P \land Q)$ is logically equivalent to $\neg P \lor \neg Q$ (3 points)

4 Functions (5 points)

- 1. Consider $f: \mathbb{R} \to \mathbb{R}$ such that f(x) = 5x 7.
 - (a) Prove that f is invertible. (2 points)

(b) Find f^{-1} . (1 point)

2. Let $S = \mathbb{N}$ and let $A = \{1, 2, 3, 4, 5\}$. Consider $\chi_A : \mathbb{N} \to \{0, 1\}$. Prove that χ_A is onto, but is **NOT** one-to-one. (2 points)