CIS 32 Homework 4

Fall 2003

- 1. Using the proof rules in the lecture notes and those given below, try to prove the following:
 - (a) $(p, p \Rightarrow (q \land r)) \vdash (p \lor r)$
 - (b) $(p \land (p \Rightarrow (q \land r))) \vdash (p \lor r)$
 - (c) $(p \land (p \Rightarrow (q \land r))) \vdash (s \lor r)$

(45 points)

Some proof rules that aren't in the lecture notes are:

$$\begin{array}{c} \vdash \phi \Leftrightarrow \psi \\ \hline \vdash \phi \Rightarrow \psi; \vdash \psi \Rightarrow \phi \end{array} \Leftrightarrow -\mathbf{E} \\ \\ \hline \hline \vdash \phi \Rightarrow \psi; \vdash \psi \Rightarrow \phi \\ \hline \hline \vdash \phi \Leftrightarrow \psi \end{array} \Leftrightarrow -\mathbf{I} \\ \\ \hline \hline \hline \vdash \phi \Leftrightarrow \psi \end{array} \to -\mathbf{E} \\ \\ \hline \hline \phi \vdash \bot \\ \hline \hline \vdash \neg \phi \end{array} \neg -\mathbf{I}$$

For the last of these rules, remember that \perp stands for any formula which is inconsistent (for example $\phi \land \neg \phi$).

- 2. Convert the following sentences to predicate logic form:
 - (a) Every prime number other than 2 is odd.
 - (b) Every cloud has a silver lining.
 - (c) Nobody knows the trouble I seen.
 - (d) Everybody hates grunge music.

(e) Everybody hates all grunge music except that by Nirvana.

(20 points)

3. Let

Days(x)	mean that x is a day
R(x)	mean that x is rainy
S(x)	mean that x is sunny

Symbolise each of the following in two different ways:

- (a) Every day is sunny.
- (b) Some days are not sunny.
- (c) Every day that is not sunny is rainy.

(15 points)

4. Prove $(p, p \Rightarrow (q \land r)) \vdash (p \lor r)$ using resolution. (20 points)