

Overview

Aims of this lecture:

• show how basic search (depth 1st, breadth 1st) can be improved;

• introduce:

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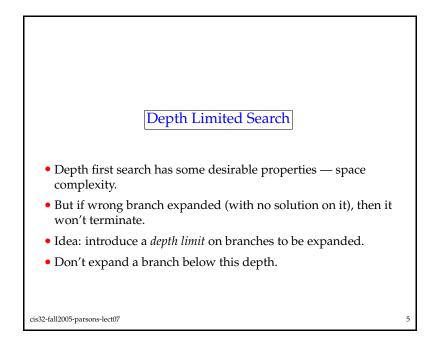
- *depth limited search;*
- iterative deepening.
- show that even with such improvements, search is hopelessly unrealistic for real problems.

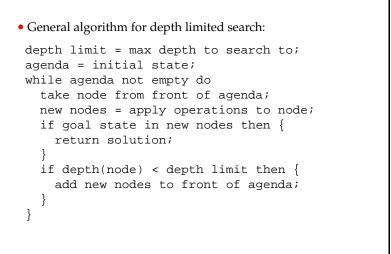
Algorithmic Improvements

- Are then any *algorithmic* improvements we can make to basic search algorithms that will improve overall performance?
- Try to get *optimality* and *completeness* of breadth 1st search with *space efficiency* of depth 1st.
- Not too much to be done about time complexity :-(

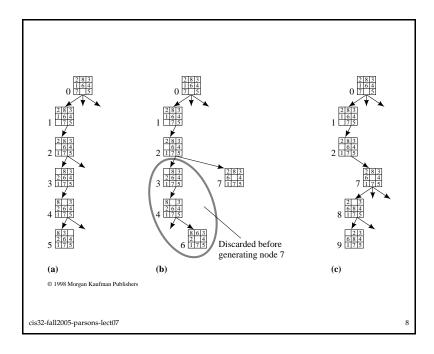
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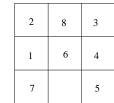


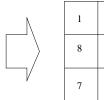


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• For the 8-puzzle setup as:





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• the search will be as follows:

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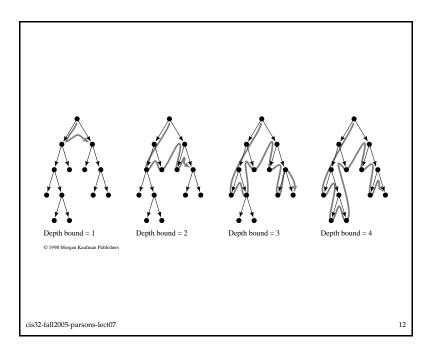
- So, when we hit the depth bound, we don't add any more nodes to the agenda.
- Then we pick the next node off the agenda.
- This has the effect of moving the search back to the last node above depth limit that that is "partly expanded".
- This is known as *chronological backtracking*.
- The effect of the depth limit is to force the search of the whole state space down to the limit.
- We get the completeness of breadth-first (down to the limit), with the space cost of depth first.

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• General algorithm for depth limited search:
depth limit = 1;
repeat {
    result = depth_limited_search(
        max depth = depth limit;
        agenda = initial node;
    );
    if result contains goal then {
        return result;
    }
    depth limit = depth limit + 1;
    } until false; /* i.e., forever */
• Calls d.l.s. as subroutine.
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Iterative Deepening Unfortunately, if we choose a max depth for d.l.s. such that shortest solution is longer, d.l.s. is not complete. Iterative deepening an ingenious *complete* version of it. Basic idea is: do d.l.s. for depth 1; if solution found, return it; otherwise do d.l.s. for depth n; if solution found, return it; otherwise, … So we *repeat* d.l.s. for all depths until solution found.



- Note that in iterative deepening, we *re-generate nodes on the fly*.
 Each time we do call on depth limited search for depth *d*, we need to regenerate the tree to depth *d* − 1.
- Isn't this inefficient?
- Tradeoff *time* for *memory*.
- In general we might take a *little* more time, but we save a *lot* of memory.
- Now for breadth-first search to level *d*:

$$N_{bf} = 1 + b + b^{2} + b$$
(1)
= $\frac{b^{d+1} - 1}{b - 1}$ (2)

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• For large *d*:

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$$\frac{N_{id}}{N_{bf}} = \frac{b}{b-1} \tag{7}$$

- So for high branching and relatively deep goals we do a small amount more work.
- Example: Suppose b = 10 and d = 5.

Breadth first search would require examining 111, 111 nodes, with memory requirement of 100, 000 nodes. Iterative deepening for same problem: 123, 456 nodes to be searched, with memory requirement only 50 nodes. Takes 11% longer in this case. • In contrast a complete depth-limited search to level *j*:

$$N_{df}^{j} = \frac{b^{j+1} - 1}{b - 1} \tag{3}$$

• (This is just a breadth-first search to depth *j*.)

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• In the worst case, then we have to do this to depth *d*, so expanding:

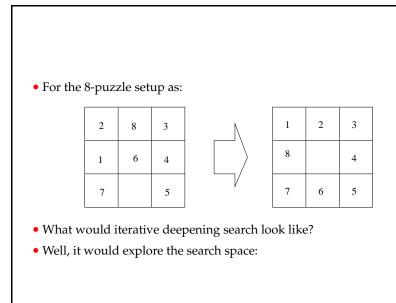
$$N_{id} = \sum_{j=0}^{d} \frac{b^{j+1} - 1}{b - 1}$$
(4)

$$=\frac{b^{d+2}-2b-bd+d+1}{(b-1)^2}$$
(6)

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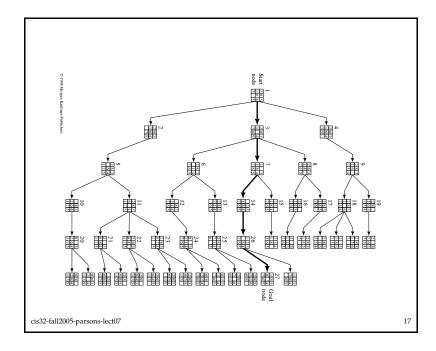
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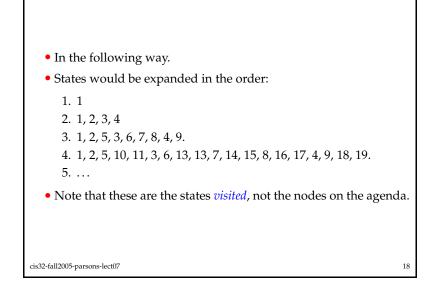
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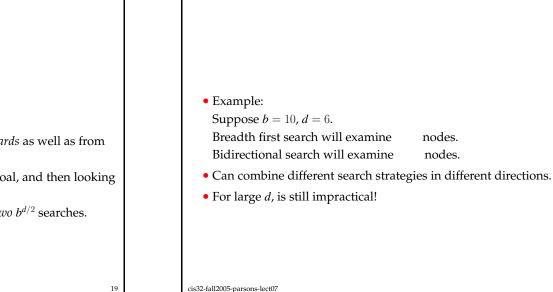
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Bi-directional Search

- Suppose we search from *the goal state backwards* as well as from *initial state forwards*.
- Involves determining *predecessor* nodes to goal, and then looking at predecessor nodes to this, ...
- Rather than doing one search of b^d , we do *two* $b^{d/2}$ searches.
- *Much* more efficient.

