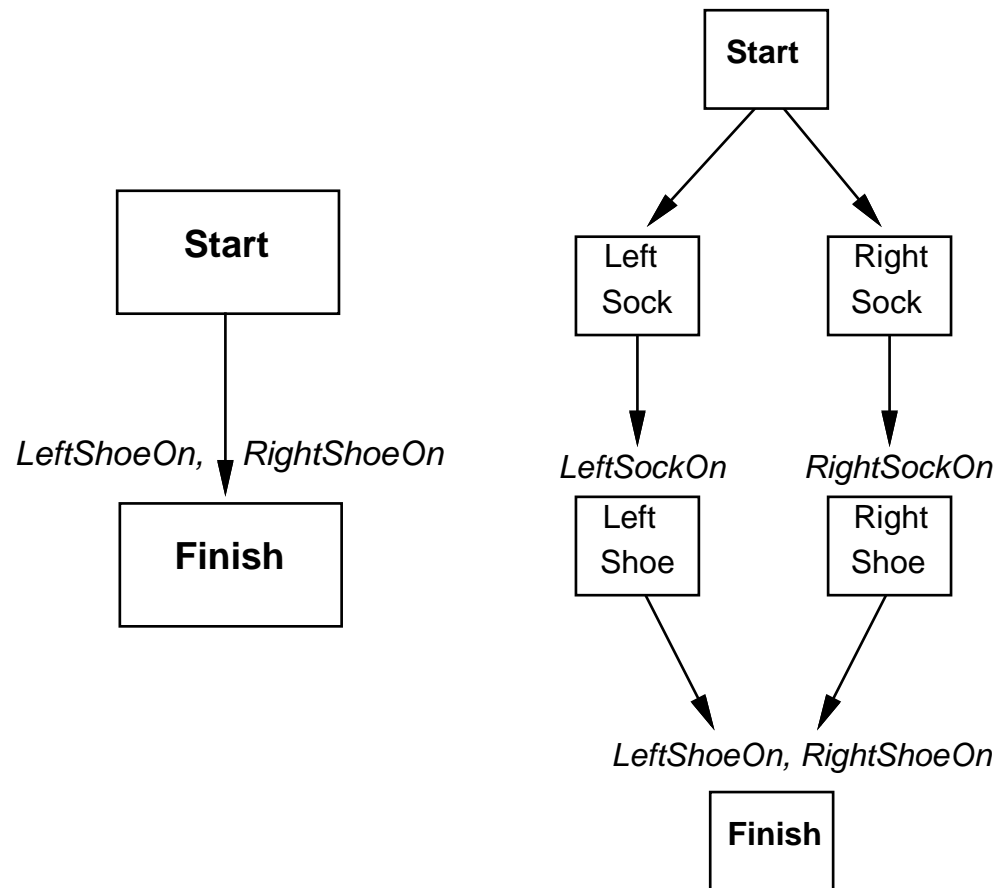


# PARTIAL-ORDER PLANNING

## Partial Order Planning

- The answer to the problem we ended the last lecture with is to use partial order planning.
- Basically this gives us a way of checking before adding an action to the plan that it doesn't mess up the rest of the plan.
- The problem is that in this recursive process, we don't know what the rest of the plan is.
- Need a new representation *partially ordered plans*.

# Representation



## Partially ordered plans

- *Partially ordered* collection of steps with
  - *Start* step has the initial state description as its effect
  - *Finish* step has the goal description as its precondition
  - *causal links* from outcome of one step to precondition of another
  - *temporal ordering* between pairs of steps
- *Open condition* = precondition of a step not yet causally linked
- A plan is *complete* iff every precondition is achieved
- A precondition is *achieved* iff it is the effect of an earlier step and no *possibly intervening* step undoes it

# Plan construction

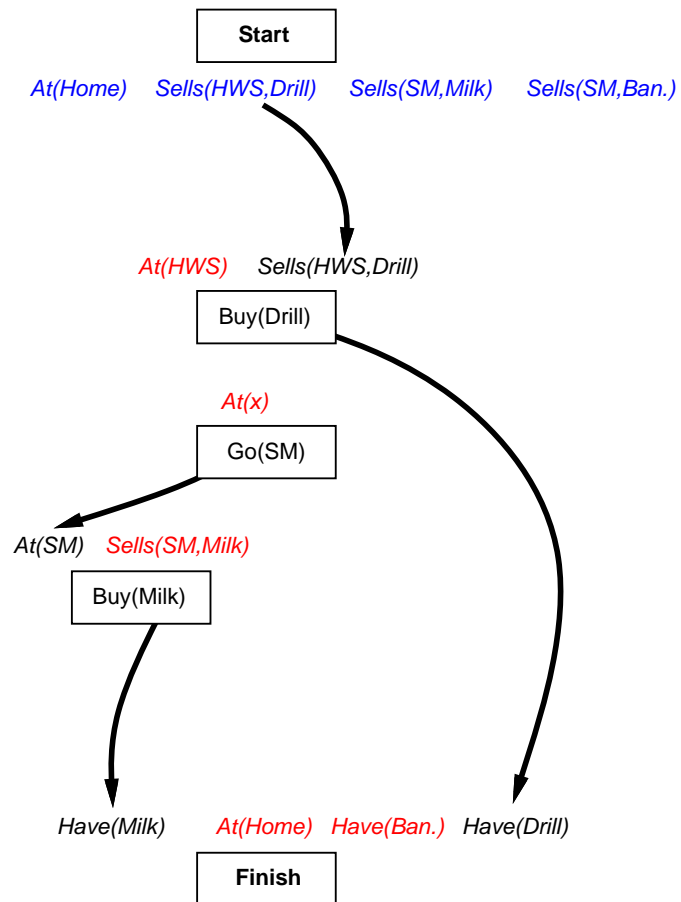
**Start**

*At(Home) Sells(HWS,Drill) Sells(SM,Milk) Sells(SM,Ban.)*

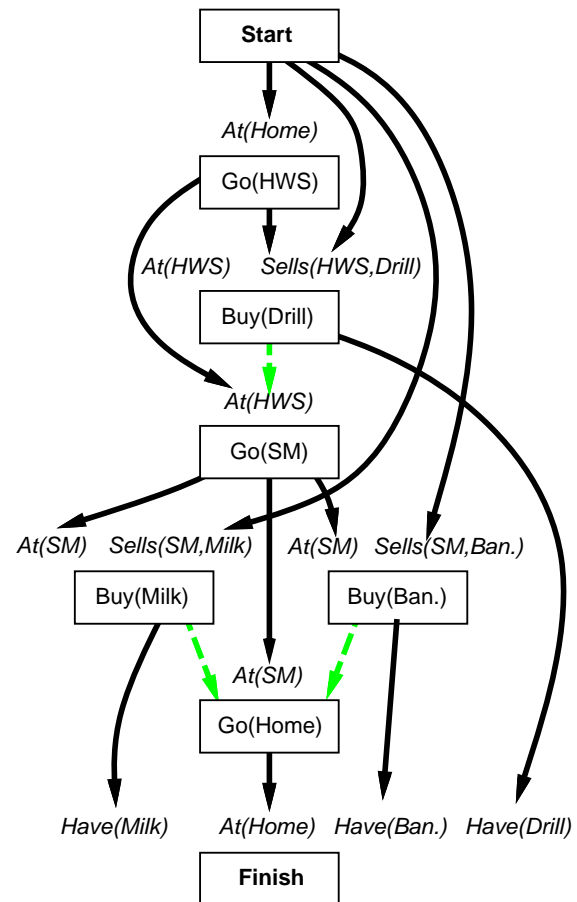
*Have(Milk) At(Home) Have(Ban.) Have(Drill)*

**Finish**

## Plan construction (2)



## Plan construction (3)



## Planning process

- Operators on partial plans:
  - *add a link* from an existing action to an open condition
  - *add a step* to fulfill an open condition
  - *order* one step wrt another to remove possible conflicts
- Gradually move from incomplete/vague plans to complete, correct plans
- Backtrack if an open condition is unachievable or if a conflict is unresolvable



## POP algorithm

**function** POP(*initial*, *goal*, *operators*) **returns** *plan*

*plan*  $\leftarrow$  MAKE-MINIMAL-PLAN(*initial*, *goal*)

**loop do**

**if** SOLUTION?(*plan*) **then return** *plan*

$S_{need}, c \leftarrow$  SELECT-SUBGOAL(*plan*)

    CHOOSE-OPERATOR(*plan*, *operators*,  $S_{need}$ ,  $c$ )

    RESOLVE-THREATS(*plan*)

**end**

---

**function** SELECT-SUBGOAL(*plan*) **returns**  $S_{need}, c$

    pick a plan step  $S_{need}$  from STEPS(*plan*)

        with a precondition  $c$  that has not been achieved

**return**  $S_{need}, c$

**procedure** CHOOSE-OPERATOR( $plan, operators, S_{need}, c$ )

**choose** a step  $S_{add}$  from  $operators$  or STEPS( $plan$ ) that has  $c$  as an effect

**if** there is no such step **then fail**

  add the causal link  $S_{add} \xrightarrow{c} S_{need}$  to LINKS( $plan$ )

  add the ordering constraint  $S_{add} \prec S_{need}$  to ORDERINGS( $plan$ )

**if**  $S_{add}$  is a newly added step from  $operators$  **then**

    add  $S_{add}$  to STEPS( $plan$ )

    add  $Start \prec S_{add} \prec Finish$  to ORDERINGS( $plan$ )

---

**procedure** RESOLVE-THREATS( $plan$ )

**for each**  $S_{threat}$  that threatens a link  $S_i \xrightarrow{c} S_j$  in LINKS( $plan$ ) **do**

**choose** either

*Demotion:* Add  $S_{threat} \prec S_i$  to ORDERINGS( $plan$ )

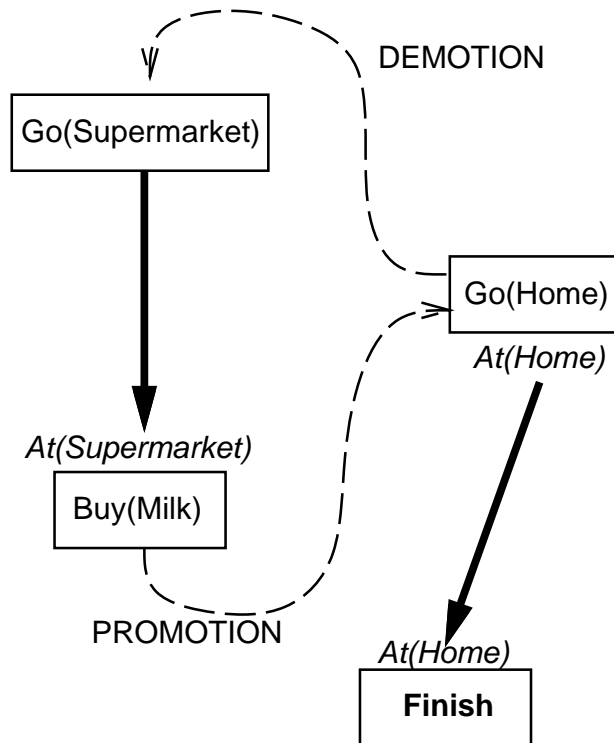
*Promotion:* Add  $S_j \prec S_{threat}$  to ORDERINGS( $plan$ )

**if not** CONSISTENT( $plan$ ) **then fail**

**end**

## Clobbering

- A *clobberer* is a potentially intervening step that destroys the condition achieved by a causal link. E.g.,  $Go(Home)$  clobbers  $At(Supermarket)$ :



*Demotion*: put before  $Go(Supermarket)$

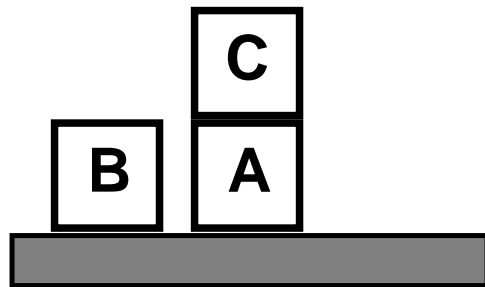
*Promotion*: put after  $Buy(Milk)$

## Properties of POP

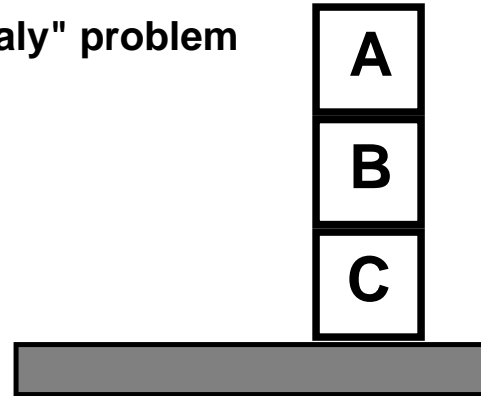
- Nondeterministic algorithm: backtracks at *choice* points on failure:
  - choice of  $S_{add}$  to achieve  $S_{need}$
  - choice of demotion or promotion for clobberer
  - selection of  $S_{need}$  is irrevocable
- POP is sound, complete, and *systematic* (no repetition)
- Extensions for disjunction, universals, negation, conditionals
- Can be made efficient with good heuristics derived from problem description
- Particularly good for problems with many loosely related subgoals

## Example

"Sussman anomaly" problem



Start State



Goal State

*Clear(x) On(x,z) Clear(y)*

PutOn(x,y)

$\sim On(x,z) \sim Clear(y)$   
 $Clear(z) On(x,y)$

*Clear(x) On(x,z)*

PutOnTable(x)

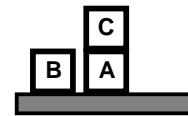
$\sim On(x,z) Clear(z) On(x, Table)$

+ several inequality constraints

## Example (2)

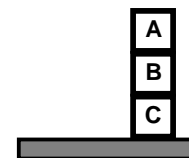
START

*On(C,A) On(A,Table) Cl(B) On(B,Table) Cl(C)*

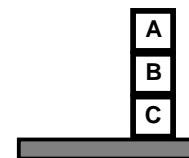
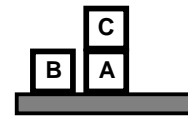
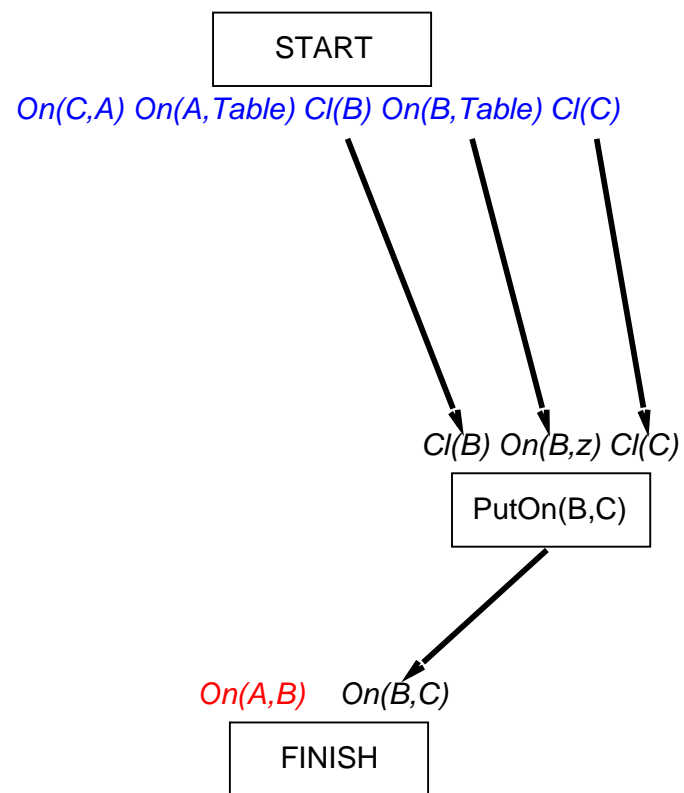


*On(A,B) On(B,C)*

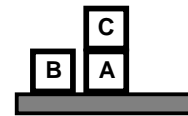
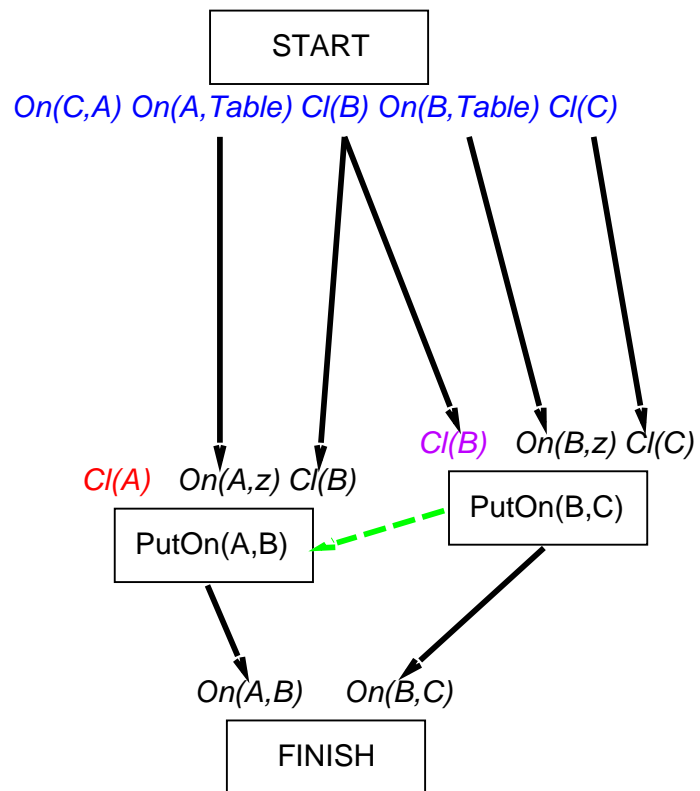
FINISH



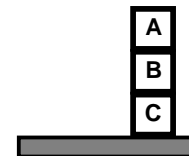
## Example (3)



## Example (4)

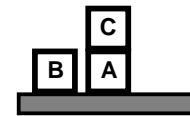
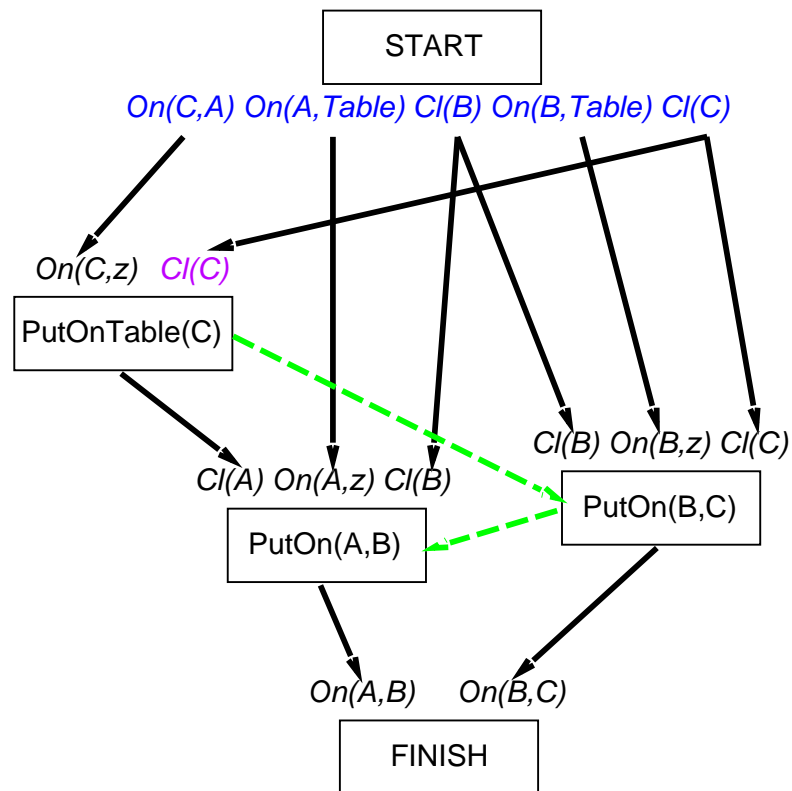


PutOn(A,B)  
 clobbers Cl(B)  
 => order after  
 PutOn(B,C)



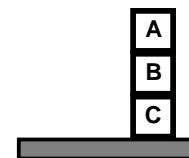


## Example (5)



PutOn(A,B)  
clobbers Cl(B)  
=> order after  
PutOn(B,C)

PutOn(B,C)  
clobbers Cl(C)  
=> order after  
PutOnTable(C)



## Summary

- This lecture has looked at a more advanced approach to planning.
  - Partial order planning
- This requires a new way of looking at the world, but the payoff is a more robust approach.
- We also looked at the POP algorithm, ...
- ...and saw how it could solve the Sussman anomaly.