GAME PLAYING

- In other words we can plan when the world is:
 - Accessible;
 - Deterministic; and
 - Static
- Obviously these are unrealistic simplifications.
- Here we will consider how to handle one kind of dynamism:
 - Other agents messing with the world.
- (In later lectures we will work towards dealing with other kinds of complication.)

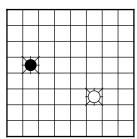
Adversarial search

- One of the reasons we use search in AI is to help agents figure out what to do.
- As we mentioned before, considering how sequences of actions can be put together allows the agent to plan.
- (We will come back to this topic again in a few lectures' time).
- Using the techniques we have covered so far, we can have a single agent figure out what to do when:
 - It knows exactly how the world is;
 - Each action only has one outcome; and
 - The world only changes when the agent makes it change.

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• Consider a set up where we have two agents moving in the grid world:



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• We assume that agents take it in turn to move.

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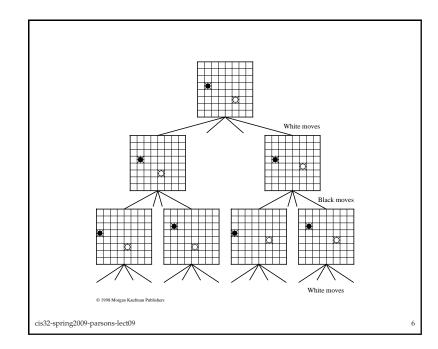
- One typical kind of scenario which fits this profile is a two-person game.
- Consider that White wants to be in the same cell as Black.
- Black wants to avoid this.
- (These could be moves in a chess endgame.)
- What each agent wants is a move that guarantees success whatever the other does.
- Usually all they can find is a move that improves things from their point of view.

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Computers and Games

- This example is a *two person*, *perfect information*, *zero sum* game.
- Perfect information:
 - Both players know exactly what the state of the game is.
- Zero sum:
 - What is good for one player is bad for the other.
- \bullet This is also true of chess, draughts, go, othello, connect 4, \dots



- These games are relatively easy to study at an introductory level.
- They have been studied just about as long as AI has been a subject.
- Some games are easily "solved":
 - Tic-Tac-Toe
- Others have held out until recently.
 - Checkers
 - Chess
- Yet others are far from being mastered by computers.
 - Go
- Chance provides another complicating element.

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- For many of these games
 - State space
 - Iconic

representations seem natural.

- Moves are represented by state space operators.
- Search trees can be built much as before.
- However, we use different techniques to choose the optimal moves.

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- We can't search the whole tree:
 - Chess: 10⁴⁰ nodes
 - $-\approx 10^{20}$ centuries to build search tree.
- So just search to a limited horizon (like depth-bounded).
- Then evaluate (using some heuristic) the leaf nodes.
- Then extract the best move at the top level.
- How do we do this (and how do we take into account the fact that MIN is also trying to win)?
- We use the minimax procedure.

Minimax procedure

- Typically we name the two players MAX and MIN.
- MAX moves first, and we want to find the best move for MAX.
- Since MAX moves first, even numbered layers are the ones where MAX gets to choose what move to make.
- The first node is on the zeroth layer.
- We call these "MAX nodes".
- "Min nodes" are defined similarly.
- A *ply* of *ply-depth* k are the nodes at depth 2k and 2k + 1.
- We usually estimate, in ply, the depth of the "lookahead" performed by both agents.

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- Assume our heuristic gives nodes high positive values if they are good for MAX
- And low values if they are good for MIN.
- Now, look at the leaf nodes and consider which ones MAX wants:
 - Ones with high values.
- MAX could choose these nodes *if* it was his turn to play.
- So, the value of the MAX-node parent of a set of nodes is the max of all the child values.

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- Similarly, when MIN plays she wants the node with the lowest value.
- So the MIN-node parent of a set of nodes gets the min of all their values
- We back up values until we get to the children of the start node, and MAX can use this to decide which node to choose.
- There is an assumption (another!) which is that the evaluation function works as a better guide on nodes down the tree than on the direct successors of the start node.
- This should be the case (modulo horizon effects).
- Let's look at a concrete example—Tic-Tac-Toe.

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So,

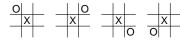


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• Scores:

$$6 - 4 = 2$$

• We also use symmetry to avoid having to generate loads of successor states, so



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- are all equivalent.
- So, run the depth 2 search, evaluate, and back up values

• Let MAX play crosses and go first.

- Breadth-first search to depth 2.
- evaluation function e(p):

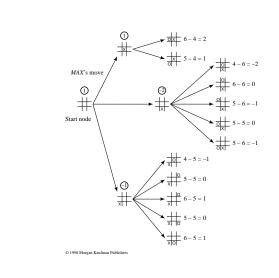
$$e(p) = \begin{cases} \infty & \text{if } p \text{ is a win for MAX} \\ -\infty & \text{if } p \text{ is a win for MIN} \\ val & \text{otherwise} \end{cases}$$

where

val = (possible winning rows columns diagonals for MAX)-(possible winning rows columns diagonals for MIN)

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• Unsurprisingly (for anyone who ever played Tic-Tac-Toe):

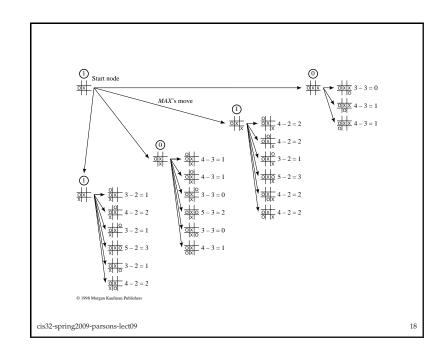


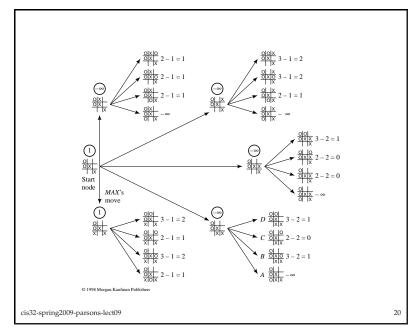
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- Is the best move.
- So MAX moves and then MIN replies, and then MAX searches again:

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- Here there are two equally good best moves.
- So we can break the tie randomly.
- Then we let MIN move and do the search again.





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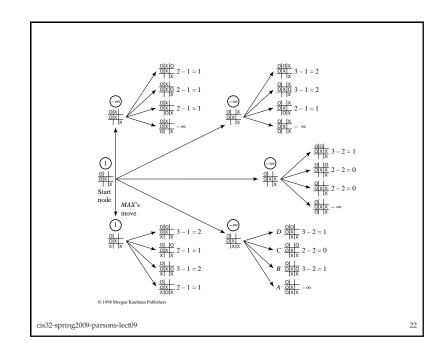
Alpha-Beta search

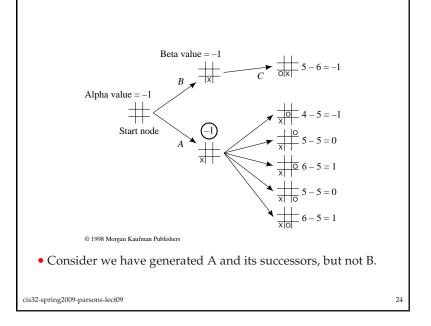
- Minimax works very neatly, but it is inefficient.
- The inefficiency comes from the fact that we:
 - Build the tree,
 - THEN back up the values
- If we combine the two we get massive savings in computation.
- How do we manage this?

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- Well, when we get to node A, we don't have to expand any further.
- So we save the evaluation of B, C and D.
- We also don't have to search any of the nodes below these nodes.
- This does nothing to stop MAX finding the best move.
- It also works when we don't have a winning move for MIN.
- Consider the following (earlier) stage of Tic-Tac-Toe.





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- Node A has backed-up value -1.
- Thus the start node cannot have a lower value than -1.
- This is the *alpha* value.
- Now let's go on to B and C.
- Since C has value -1, B cannot have a greater value than -1.
- This is the *beta* value.
- In this case, because B cannot ever be better than A, we can stop the expansion of B's children.

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- We compute the values as:
 - Alpha: current largest final backed-up value of successors.
 - Beta: current smallest final backed-up value of successors.
- We keep searching until we meet the "stop seach" *cut-off* rules, or we have backed-up values for all the sucessors of the start node.
- Doing this always gives the same best move as full minimax.
- However, often (usually) this alpha-beta approach involves less searching.

- In general:
 - Alpha values of MAX nodes can never decrease.
 - Beta values of MIN nodes can never increase.
- Thus we can stop searching below:
 - Any MIN node with a beta value less than or equal to the alpha value of one of its MAX ancestors.
 - The backed up value of this MIN can be set to its beta value.
 - Any MAX node with an alpha value greater than or equal to any of its MIN node ancestors.
 - The backed up value of this MAX node can be set to its alpha value.

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Horizon effects

- How do we know when to stop searching?
- What looks like a very good position for MAX might be a very bad position just over the horizon.
- Stop at *quiescent* nodes (value is the same as it would be of you looked ahead a couple of moves).
- Can be exploited by opponents; pushing moves back behind the horizon.
- A similar problem occurs because we assume that players always make their best move:
 - "Bad" moves can mislead a minimax-style player.

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Games of chance

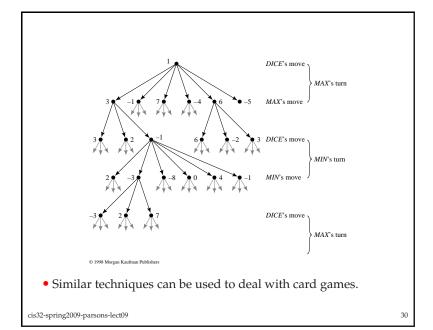
- How do we handle dice games?
- A neat trick is to model this as a another player DICE.
- We back up values in the usual way, maximising for MAX and minimising for MIN.
- For DICE moves, we back up the expected (weighted average) of the moves.
- For a single die, the weight is 1/6.
- For more complex situations we use whatever probability distribution is indicated.

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Summary

- We have looked at game playing as adversarial state-space search.
- Minimax search is the basic technique for finding the best move.
- Alpha/beta search gives greater efficiency.
- Games of chance can be handled by adding in the random player DICE or DEALER.



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