LOCAL SEARCH AND CONSTRAINT SATISFACTION

Introduction

- We have already looked in some detail at search techniques.
 - Next lecture we'll go on and look at adversartial search.
- However, there are a couple of other topics we should look at before we get to adversarial search.
 - Local search
 - Constraint satisfaction

both of which permeate artificial intelligence.

• They are also useful techniques for all computer scientists to know.

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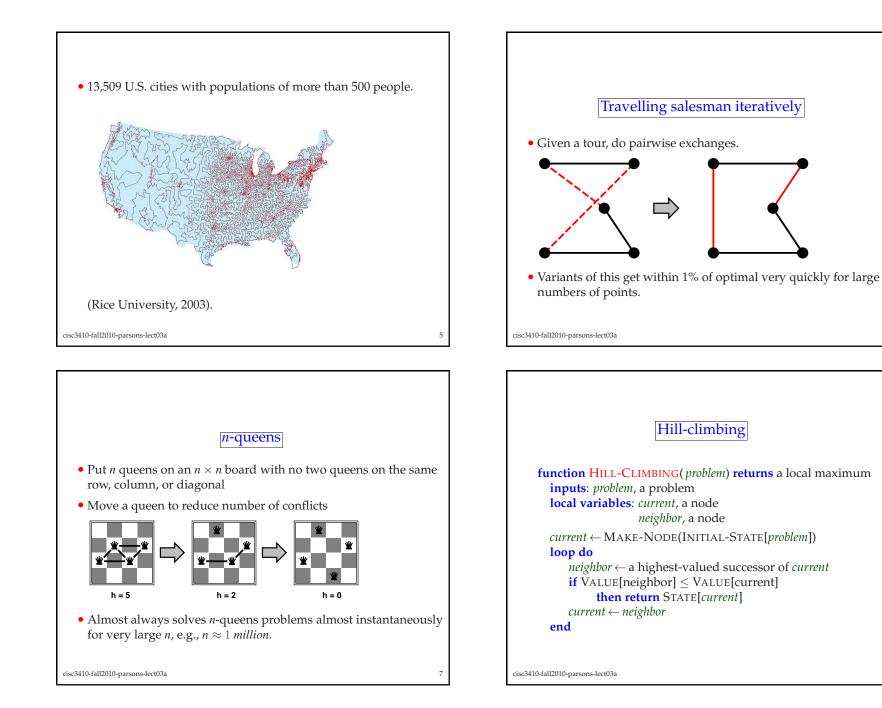
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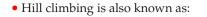
Travelling salesman • Problem is to visit all cities once while travelling the shortest distance. Seattle Portlan www.York City Salt Lake Cit San Francisco •Las Vegas os Angeles Atlar cisc3410-fall2010-parsons-lect03a

Iterative improvement

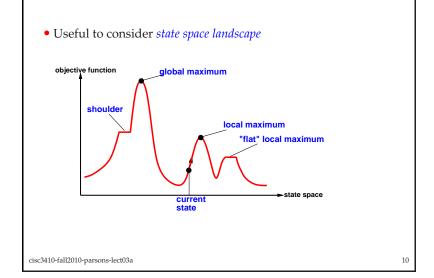
- For many problems, the *path* is irrelevant, we just want to find the goal state.
 - Optimization problems
- The state space is the set of configurations.
- We want:
 - the optimum configuration.
 - a configuration that satisfies constraints
- In these cases we can take any state and work to improve it.
 - "Local" since only keep a small part of the state space.
- Constant space.

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- Gradient ascent.
- Gradient descent.
- Like climbing a hill in the fog with amnesia.
 - All you can do is keep heading up until you get to the top.



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- *Random-restart hill climbing* overcomes local maxima—trivially complete.
 - Eventually you start from the bottom of every hill.
- *Random sideways moves* escapes from shoulders but loops on flat maxima

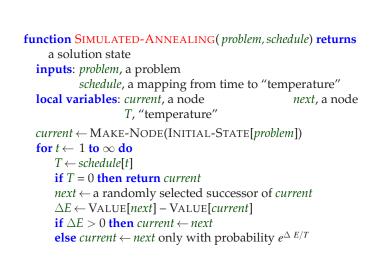
Simulated annealing

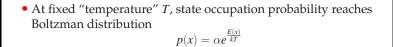
• Idea: escape local maxima by allowing some "bad" moves

but gradually decrease their size and frequency

• The random jumping around should mean that, over time, we find the highest maximum.

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$$e^{\frac{E(x^*)}{kT}}/e^{\frac{E(x)}{kT}} = e^{\frac{E(x^*)-E(x)}{kT}} \gg 1$$

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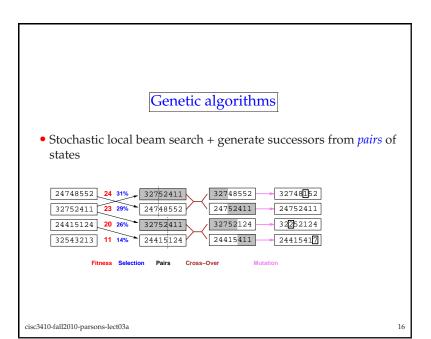
for small *T*

• Widely used in VLSI layout, airline scheduling, etc.

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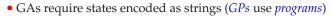
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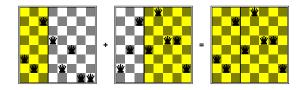
Local beam search

- Idea: keep *k* states instead of 1; choose top *k* of all their successors
- Not the same as *k* searches run in parallel!
 - Searches that find good states recruit other searches to join them.
- Problem: quite often, all *k* states end up on same local hill
- Idea: choose *k* successors randomly, biased towards good ones
- Observe the close analogy to natural selection!

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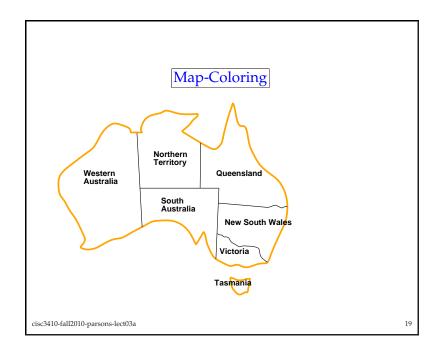


• Crossover helps *iff substrings are meaningful components*



- GAs \neq evolution
 - real genes encode replication machinery!

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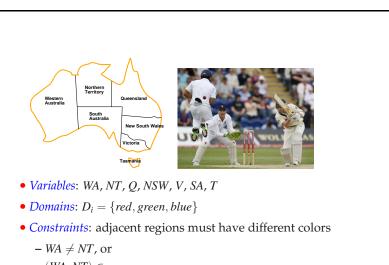


Constraint satisfaction

- Another approach to optimization.
- In standard search problems a *state* is a "black box"—any old data structure that supports goal test, eval, successor
- In CSP a *state* is defined by *variables* X_i with *values* from a *domain* D_i
- The *goal test* is a set of *constraints* specifying allowable combinations of values for subsets of variables.
- Simple example of a *formal representation language*.
- Allows useful *general-purpose* algorithms with more power than standard search algorithms

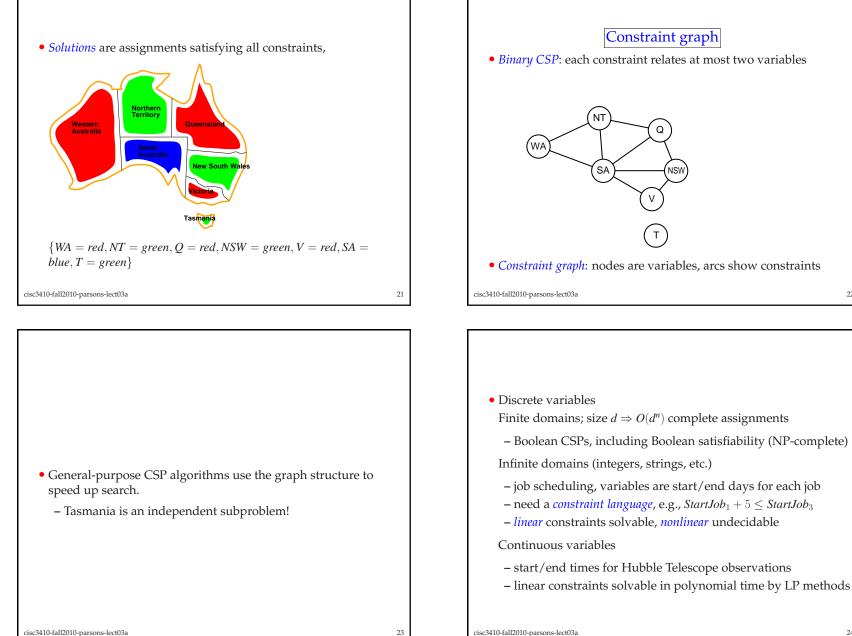
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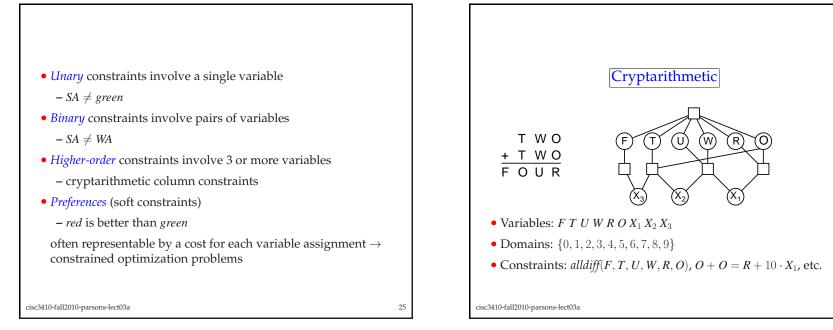
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 $\begin{array}{l} \textbf{-} (\textit{WA},\textit{NT}) \in \\ \{(\textit{red},\textit{green}),(\textit{red},\textit{blue}),(\textit{green},\textit{red}),(\textit{green},\textit{blue}),\ldots\} \end{array}$

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Real-world CSPs

- Assignment problems
 - who teaches what class
- Timetabling problems
 - which class is offered when and where?
- Hardware configuration
- Spreadsheets
- Transportation scheduling
- Factory scheduling
- Floorplanning

Notice that many real-world problems involve real-valued variables

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Standard search formulation

- Let's start with the straightforward, dumb approach, then fix it
- States are defined by the values assigned so far
 - Initial state: the empty assignment, { }
 - Successor function: assign a value to an unassigned variable that does not conflict with current assignment. ⇒ fail if no legal assignments (not fixable!)
 - Goal test: the current assignment is complete
- This is the same for all CSPs!
- Every solution appears at depth *n* with *n* variables ⇒ use depth-first search
- Path is irrelevant, so can also use complete-state formulation
- $b = (n \ell)d$ at depth ℓ , hence $n!d^n$ leaves!

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- Variable assignments are *commutative*, i.e., [*WA* = *red* then NT = green] same as [*NT* = *green* then *WA* = *red*]
- Only need to consider assignments to a single variable at each node so *b* = *d* and there are *dⁿ* leaves.
- Depth-first search for CSPs with single-variable assignments is called *backtracking* search
- Backtracking search is the basic uninformed algorithm for CSPs
- Can solve *n*-queens for $n \approx 25$.

function RECURSIVE-BACKTRACKING(assignment, csp) returns soln/failure if assignment is complete then return assignment $var \leftarrow Select-UNASSIGNED-VARIABLE$ (VARIABLES[*csp*], *assignment*, *csp*) **for each** *value* **in** ORDER-DOMAIN-VALUES(*var*, *assignment*, *csp*) do **if** *value* is consistent with *assignment* given CONSTRAINTS[*csp*] then add {*var* = *value*} to *assignment result* \leftarrow RECURSIVE-BACKTRACKING(*assignment*, *csp*) **if** result \neq failure **then return** result remove {*var* = *value*} from *assignment* **return** failure cisc3410-fall2010-parsons-lect03a 31 function BACKTRACKING-SEARCH(csp) returns solution/failure
return RECURSIVE-BACKTRACKING({ }, csp)

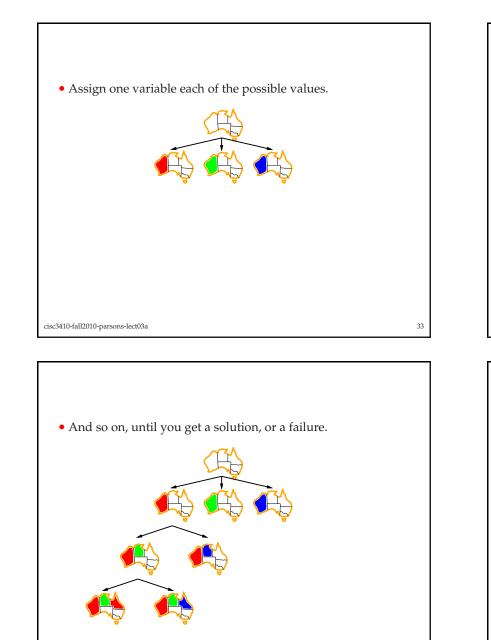
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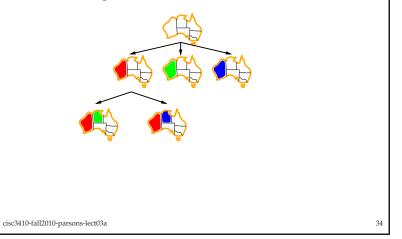
• No variables assigned values.



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• Then take one of those proto-solutions and assign another variable each possible value.



- The search has the name *backtracking* because of what happens when the solution fails.
- Search jumps back to the most recent branch point.
 - The "back track"
- Does this method of searching remind you of anything we have seen already?

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