PROBLEM SOLVING AGENTS

Problem Solving Agents

- Lecture 1 introduced rational agents.
- Now consider agents as *problem solvers*: Systems which set themselves *goals* and find *sequences of actions* that achieve these goals.
- What is a problem?A *goal* and a *means* for achieving the goal.
- \bullet The goal specifies the state of affairs we want to bring about.
- The means specifies the operations we can perform in an attempt to bring about the means.
- The difficulty is deciding which operations and what *order* to carry out the operations.

Overview

Aims of the this lecture:

- introduce problem solving;
- introduce goal formulation;
- show how problems can be stated as state space search;
- show the importance and role of abstraction;
- introduce *undirected search*:
 - breadth 1st search;
 - depth 1st search.
- define main performance measures for search.

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• Operation of problem solving agent:

```
/* s is sequence of actions */
repeat {
    percept = observeWorld();
    state = updateState(state, p);
    if s is empty then {
        goal = formulateGoal(state);
        prob = formulateProblem(state, goal);
        s = search(prob);
    }
    action = first(s);
    s = remainder(s);
}
until false; /* i.e., forever */
```

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• Key difficulties:

```
- formulateGoal(...)
- formulateProblem(...)
```

- search(...)
- It isn't easy to see how to tackle any of these.
- Here we will concentrate mainly on search.

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Problem Formulation

- Once goal is determined, formulate the problem to be solved.
- First determine set of possible states *S* of the problem.
- Then problem has:
 - *initial state* the starting point, s_0 ;
 - *operations* the actions that can be performed, $\{o_1, \ldots, o_n\}$.
 - *goal* what you are aiming at subset of *S*.

Goal Formulation

- Where do an agent's goals come from?
 - Agent is a *program* with a *specification*.
 - Specification is to maximise performance measure.
 - Should *adopt goal* if achievement of that goal will maximise this measure.
- Goals provide a *focus* and *filter* for decision-making:
 - focus: need to consider how to achieve them;
 - *filter*: need not consider actions that are incompatible with goals.

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- The initial state together with operations determines *state space* of problem.
- Operations cause *changes* in state.
- Solution is a sequence of actions such that when applied to initial state s_0 , we have goal state.
- What does this look like?

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Examples of Toy Problems

• Example 1: The 8 puzzle.

Do the following transformation, moving tile from occupied space to filled space.

2	8	3
1	6	4
7		5



1	2	3
8		4
7	6	5

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• What state space does this define?

- Initial state as shown above.
- Goal state as shown above.
- Operations:
 - $-o_1$: move any tile to left of empty square to right;
 - $-o_2$: ?
 - $-o_3$: ?
 - $-o_4$: ?

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- Example 2: The *n* queens problem from chess.
- Place *n* queens on chess board so that no queen can be taken by another.
- Initial state: empty chess board.
- Goal state: *n* queens on chess board, one occupying each space, so that none can take others.
- Operations: place queen in empty square.

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Solution Cost

- For most problems, some solutions are better than others:
 - in 8 puzzle, number of moves to get to solution;
 - number of moves to checkmate;
 - length of distance to travel.
- Mechanism for determining *cost* of solution is *path cost function*.
- This is the length of the path through the state-space from the initial state to the goal state.

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- There are five moves:
 - 1.
 - 2.
 - 3.
 - 4.
 - 5.
- What are they?
- What does the path through the solution space look like?

• As an example, consider the following state in the 8-puzzle:

2	8	3
1	6	4
7		5

• How many moves are there to the solution?

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Problem Solving as Search

- In the state space view of the world, finding a solution is finding a path through the state space.
- When we solve a problem like the 8-puzzle we have some idea of what constitutes the next best move.
- It is hard to program this kind of approach.
- Instead we start by programming the kind of repetitive task that computers are good at.
- A *brute force* approach to problem solving involves *exhaustively searching* through the space of *all possible* action sequences to find one that achieves goal.

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- Systematically generate a *search tree*
- The tree is built by taking the initial state and identifying some states that can be obtained by applying a single operator.
- These new states become the *children* of the initial state in the tree.
- These new states are then examined to see if they are the goal state.
- If not, the process is repeated on the new states.
- We can formalise this description by giving an algorithm for it.

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- Note the difference between *state space* and *search tree*.
- State space is every possible state and the relationships between them.
 - It is static.
- Search tree the set of states the agent has looked at (is looking at) and some of the relationships between them.
 - It is dynamic.

```
• General algorithm for search:
```

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- Question: How to pick states for expansion?
- Two obvious solutions:
 - depth first search;
 - breadth first search.

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Breadth First Search

- Start by *expanding* initial state gives tree of depth 1.
- Then expand *all* nodes that resulted from previous step gives tree of depth 2.
- Then expand *all* nodes that resulted from previous step, and so on.
- Expand nodes at depth n before level n + 1.

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• For the 8-puzzle as so:

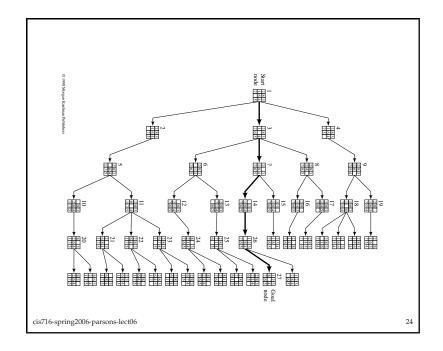
2	8	3
1	6	4
7		5

• We have the following state space:

```
/* Breadth first search */
agenda = initial state;
while agenda not empty do
{
    pick node from front of agenda;
    new nodes = apply operations to state;
    if goal state in new nodes then
    {
        return solution;
    }

    APPEND new nodes to END of agenda;
}

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```



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• Given this numbering of the states, the agenda would look like

1. 1

2. 2, 3, 4

3. 3, 4, 5

4. 4, 5, 6, 7, 8

5. 5, 6, 7, 8, 9

6. 6, 7, 8, 9, 10, 11.

7. ...

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• Time for breadth first search:

Depth	Nodes	Time
0	1	1 msec
1	11	.01 sec
2	111	.1 sec
4	11,111	11 secs
6	10^{6}	18 mins
8	10^{8}	31 hours
10	10^{10}	128 days
12	10^{12}	35 years
14	10^{14}	2500 years
20	10^{20}	3 ¹⁵ years

• Combinatorial explosion!

• Advantage: *guaranteed* to reach a solution if one exists.

• If all solutions occur at depth *n*, then this is good approach.

• Disadvantage: time taken to reach solution!

• Let *b* be *branching factor* — average number of operations that may be performed from any level.

• If solution occurs at depth *d*, then we will look at

$$1 + b + b^2 + \dots + b^d$$

nodes before reaching solution — *exponential*.

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Importance of ABSTRACTION

- When formulating a problem, it is crucial to pick the right level of *abstraction*.
- Example: Given the task of driving from New York to Boston.
- Some possible actions...
 - depress clutch;
 - turn steering wheel right 10 degrees;
- ... inappropriate level of abstraction.

Too much irrelevant detail.

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- Better level of abstraction:
 - Take the Henry Hudson Parkway north
 - Take the Cross County turnoff
- ... and so on.
- Getting abstraction level right lets you focus on the specifics of problem and is one way to combat the combinatorial explosion.
- (Tell that to Mapquest).

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```
/* Depth first search */
agenda = initial state;
while agenda not empty do
{
    pick node from front of agenda;
    new nodes = apply operations to state;
    if goal state in new nodes then
    {
        return solution;
    }

put new nodes on FRONT of agenda;
}
```

Depth First Search

- Start by expanding initial state.
- Pick one of nodes resulting from 1st step, and expand it.
- Pick one of nodes resulting from 1nd step, and expand it, and so on.
- Always expand *deepest* node.
- Follow one "branch" of search tree.

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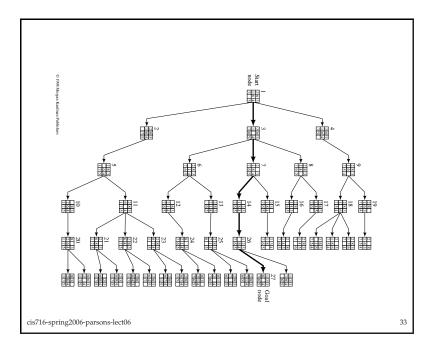
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• For the 8-puzzle as so:

2	8	3
1	6	4
7		5

• We have the following state space:

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- \bullet Given this numbering of the states, the agenda would look like
 - 1. 1
 - 2. 2, 3, 4
 - 3. 5, 3, 4
 - 4. 10, 11, 3, 4
 - 5. 20, 11, 3, 4
 - 6. ...

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- Depth first search is *not* guaranteed to find a solution if one exists.
- However, if it *does* find one, amount of time taken is much less than breadth first search.
- *Memory requirement* is much less than breadth first search.
- Solution found is *not* guaranteed to be the best.

Performance Measures for Search

• Completeness:

Is the search technique *guaranteed* to find a solution if one exists?

• Time complexity:

How many computations are required to find solution?

- *Space complexity:*How much memory space is required?
- *Optimality*: How good is a solution going to be w.r.t. the path cost function.

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Summary

- This lecture introduced the basics of problem solving.
- In particular it discussed *state space* models and looked at the basic techniques for solving them.
 - Search for the goal.
 - Path through state space is the solution.
- We also looked at two techniques for search:
 - Breadth first.
 - Depth first.

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