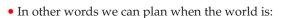


#### Adversarial search

- One of the reasons we use search in AI is to help agents figure out what to do.
- Considering how sequences of actions can be put together allows the agent to plan.
- (We will come back to this topic again in a few lectures' time).
- Using the techniques we have covered so far, we can have a single agent figure out what to do when:
  - It knows exactly how the world is;
  - Each action only has one outcome; and
  - The world only changes when the agent makes it change.

cis716-fall2005-parsons-lect09



- Accessible;
- Deterministic; and
- Static

cis716-fall2005-parsons-lect09

- Obviously these are unrealistic simplifications.
- Here we will consider how to handle one kind of dynamism:
  - Other agents messing with the world.
- (Later lectures will look at other kinds of complication.)

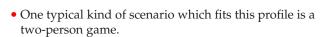
• Consider a set up where we have two agents moving in the grid world:

· ·	Ò							
	· ·							
				-	Ø			
© 19	© 1998 Morgan Kaufman Publishers							

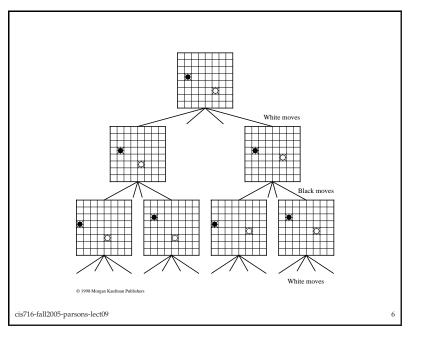
• We assume that agents take it in turn to move.

cis716-fall2005-parsons-lect09

3



- Consider that White wants to be in the same cell as Black.
- Black wants to avoid this.
- (These could be moves in a chess endgame.)
- What each agent wants is a move that guarantees success whatever the other does.
- Usually all they can find is a move that improves things from their point of view.



cis716-fall2005-parsons-lect09

# Computers and Games

- This example is a *two person*, *perfect information*, *zero sum* game.
- Perfect information:
  - Both players know exactly what the state of the game is.
- Zero sum:

cis716-fall2005-parsons-lect09

- What is good for one player is bad for the other.
- This is also true of chess, draughts, go, othello, connect 4, ...

- These games are relatively easy to study at an introductory level.
- They have been studied just about as long as AI has been a subject.
- Some games are easily "solved":
  - Tic-Tac-Toe
- Others have held out until recently.
  - Checkers
  - Chess
- Yet others are far from being mastered by computers.
  - Go
- Chance provides another complicating element.

cis716-fall2005-parsons-lect09

7

- For many of these games
  - State space
  - Iconic

representations seem natural.

- Moves are represented by state space operators.
- Search trees can be built much as before.
- However, we use different techniques to choose the optimal moves.

```
cis716-fall2005-parsons-lect09
```

- We can't search the whole tree:
  - Chess:  $10^{40}$  nodes
  - $10^{22}$  centuries to build search tree.
- So just search to a limited horizon (like depth-bounded).
- Then evaluate (using some heuristic) the leaf nodes.
- Then extract the best move at the top level.
- How do we do this (and how do we take into account the fact that MIN is also trying to win)?
- We use the minimax procedure.

## Minimax procedure

- Typically we name the two players MAX and MIN.
- MAX moves first, and we want to find the best move for MAX.
- Since MAX moves first, even numbered layers are the ones where MAX gets to choose what move to make.
- The first node is on the zeroth layer.
- We call these "MAX nodes".
- "Min nodes" are defined similarly.
- A *ply* of *ply-depth* k are the nodes at depth 2k and 2k + 1.
- We usually estimate, in ply, the depth of the "lookahead" performed by both agents.

cis716-fall2005-parsons-lect09

• Assume our heuristic gives nodes high positive values if they are good for MAX

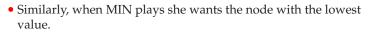
10

12

- And low values if they are good for MIN.
- Now, look at the leaf nodes and consider which ones MAX wants:
  - Ones with high values.
- MAX could choose these nodes *if* it was his turn to play.
- So, the value of the MAX-node parent of a set of nodes is the max of all the child values.

cis716-fall2005-parsons-lect09

11

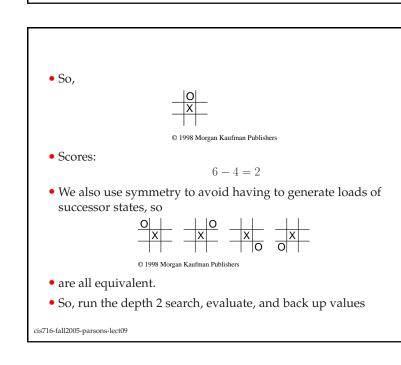


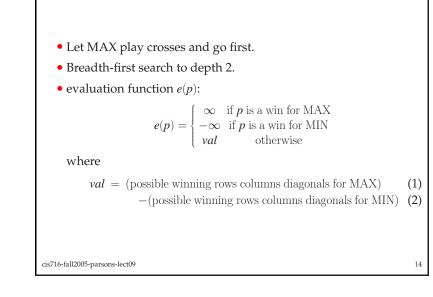
- So the MIN-node parent of a set of nodes gets the min of all their values.
- We back up values until we get to the children of the start node, and MAX can use this to decide which node to choose.
- There is an assumption (another!) which is that the evaluation function works as a better guide on nodes down the tree than on the direct successors of the start node.

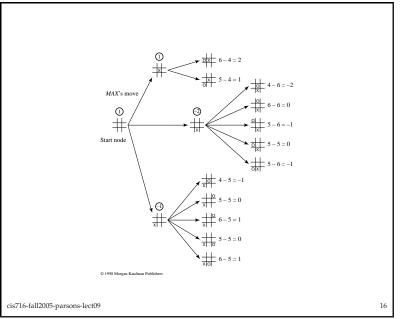
13

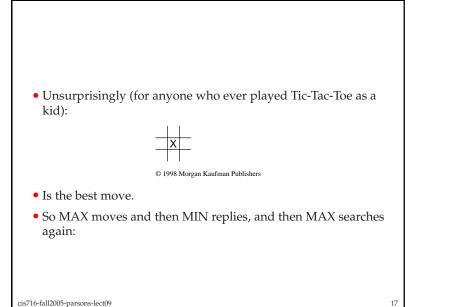
15

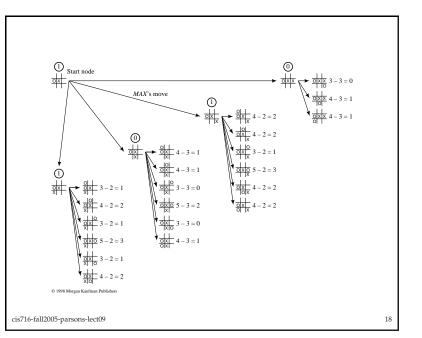
- This should be the case (modulo horizon effects).
- Let's look at a concrete example—Tic-Tac-Toe.

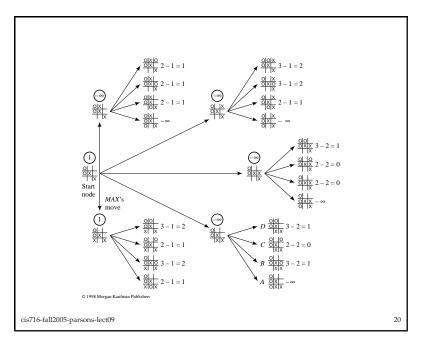












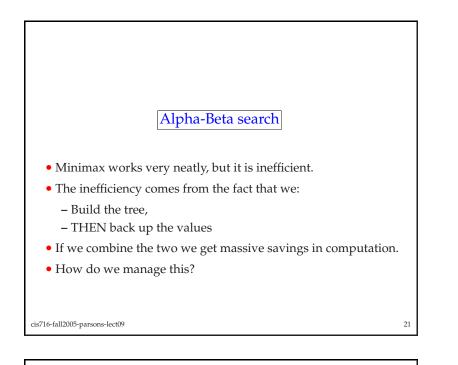
• Here there are two equally good best moves.

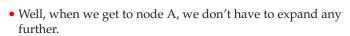
• So we can break the tie randomly.

• Then we let MIN move and do the search again.

19



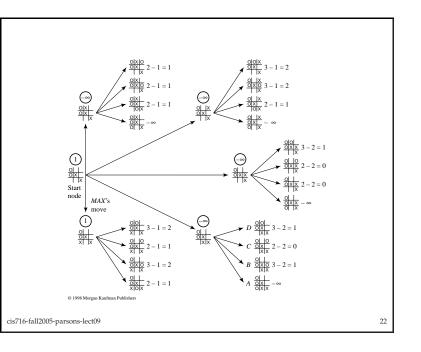


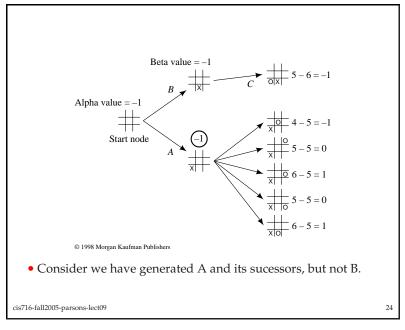


- So we save the evaluation of B, C and D.
- We also don't have to search any of the nodes below these nodes.

23

- This does nothing to stop MAX finding the best move.
- It also works when we don't have a winning move for MIN.
- Consider the following (earlier) stage of Tic-Tac-Toe.





- Node A has backed-up value -1.
- Thus the start node cannot have a lower value than -1.
- This is the *alpha* value.
- Now let's go on to B and C.
- Since C has value -1, B cannot have a greater value than -1.
- This is the *beta* value.
- In this case, because B cannot ever be better than A, we can stop the expansion of B's children.

cis716-fall2005-parsons-lect09

- We compute the values as:
  - Alpha: current largest final backed-up value of successors.
  - Beta: current smallest final backed-up value of successors.
- We keep searching until we meet the "stop seach" *cut-off* rules, or we have backed-up values for all the sucessors of the start node.
- Doing this always gives the same best move as full minimax.
- However, often (usually) this alpha-beta approach involves less searching.

- In general:
  - Alpha values of MAX nodes can never decrease.
  - Beta values of MIN nodes can never increase.
- Thus we can stop searching below:
  - Any MIN node with a beta value less than or equal to the alpha value of one of its MAX ancestors.
  - The backed up value of this MIN can be set to its beta value. - Any MAX node with an alpha value greater than or equal to
  - any of its MIN node ancestors.

The backed up value of this MAX node can be set to its alpha value.

26

28

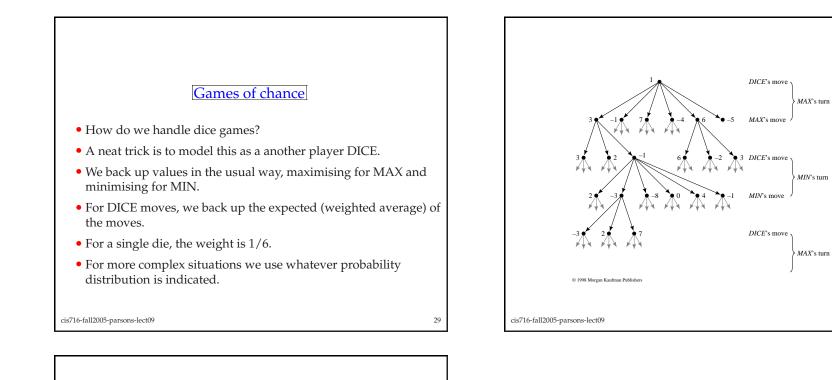
cis716-fall2005-parsons-lect09

25

27

## Horizon effects

- How do we know when to stop searching?
- What looks like a very good position for MAX might be a very bad position just over the horizon.
- Stop at *quiescent* nodes (value is the same as it would be of you looked ahead a couple of moves).
- Can be exploited by opponents; pushing moves back behind the horizon.
- A similar problem occurs because we assume that players always make their best move:
  - "Bad" moves can mislead a minimax-style player.



31

30

## Summary

- We have looked at game playing as adversarial state-space search.
- Minimax search is the basic technique for finding the best move.
- Alpha/beta search gives greater efficiency.
- Games of chance can be handled by adding in the random player DICE.