

## LECTURE 12: LOGICS FOR MULTIGENT SYSTEMS

An Introduction to Multiagent Systems

<http://www.cs.vu.ac.uk/~mjw/pubs/lmas/>

- The aim is to give an overview of the ways that theorists conceptualise agents, and to summarise some of the key developments in agent theory.
- Begin by answering the question: *why theory?*
- Discuss the various different *attitudes* that may be used to characterise agents.
- Introduce some problems associated with formalising attitudes.
- Introduce modal logic as a tool for reasoning about attitudes, focussing on knowledge/belief.
- Discuss Moore's theory of ability.
- Introduce the Cohen-Levesque theory of intention as a case study in agent theory.

## 1 Overview

development until these semantics exist.

these semantics, but progress cannot be made in language

- End users (e.g., programmers) need never read or understand

happening, or *why* it works.

- Without such a semantics, it is never clear exactly *what* is

*meaning*.

architectures, languages, and tools that we use — literally, a

- The answer is that we need to be able to give a *semantics* to the

agent based systems?

practice of software development: why should they be relevant in

- Formal methods have (arguably) had little impact of general

## 2 Why Theory?

- In agent-based systems, we have a bag of concepts and tools, which are intuitively easy to understand (by means of metaphor and analogy), and have obvious potential.
- But we need theory to reach any kind of *profound* understanding of these tools.

requires the intentional stance.

intentional systems: one whose simplest consistent description

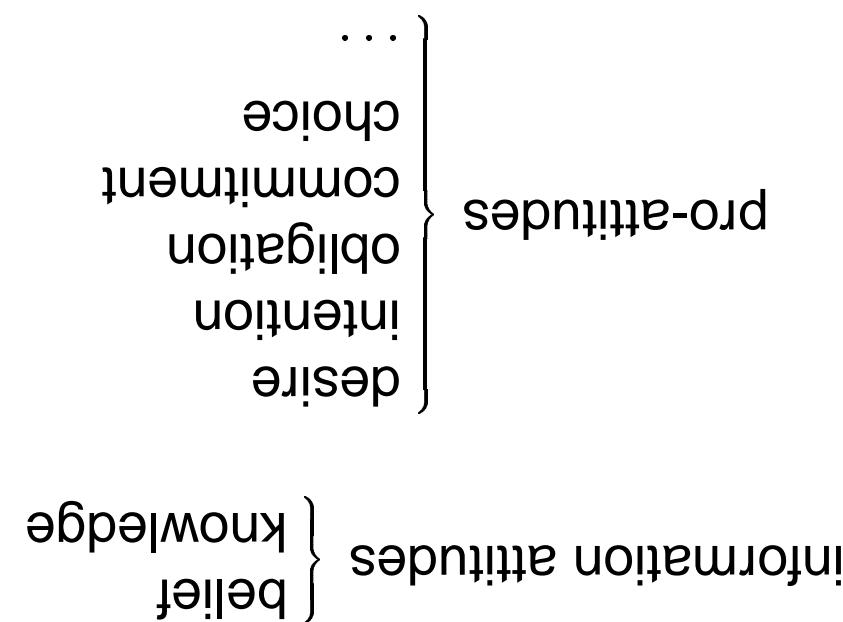
- So agent theorists start with the (strong) view of agents as
- The notion of an agent as an *intentional system*. . .
- Where do theorists start from?

### 3 Agents = Intentional Systems

- So first, *which* attitudes?
- Before we can do this, we need to identify a tractable subset of these attitudes, and a model of how they interact to generate system behaviour.
- We want to be able to design and build computer systems in terms of 'mentalist' notions.

## 4 Theories of Attitudes

- Two categories:



*intentional notions are referentially opaque.*

consider ( $Zeus = Jupiter$ )

- allows us to substitute terms with the same denotation:

*need to be able to apply  $Bel$  to formulate;*

first-order logic, not a term;

- the second argument to the  $Bel$  predicate is a *formula* of

- But . . .

$Bel(Janine, Father(Zeus, Cronos))$

- Naive translation into first-order logic:

Janine believes Cronos is father of Zeus.

- Consider . . .

- So how do we formalise attitudes?

## 5 Formalising Attitudes

- So, there are two sorts of problems to be addressed in developing a logical formalism for intentional notions:
  - a **syntactic** one (intentional notions refer to **sentences**); and
  - a **semantic** one (no substitution of equivalents).
- Thus any formalism can be characterized in terms of two attributes: its **language of formulation**, and **semantic model** [?; 83].
- Two fundamental approaches to the syntactic problem:
  - use a **modal** language, which contains **modal operators**,
  - which are applied to formulae;
  - use a **meta-language**: a first-order language containing terms that denote formulae of some other **object-language**.
- We will focus on modal languages, and in particular, **normal modal logics**, with **possible worlds semantics**.

- We introduce a (propositional) modal logic for knowledge/belief.

## 6 Normal Modal Logics

- Example formulae:

So nesting of  $K$  is allowed.

$$\begin{array}{c}
 K\langle wff \rangle \\
 | \\
 \langle wff \rangle \vee \langle wff \rangle \\
 | \\
 \neg \langle wff \rangle \\
 | \\
 \langle wff \rangle ::=\text{ any member of } \Phi
 \end{array}$$

### Syntax:

$\Phi = \{p, q, r, \dots\}$  primitive propositions  
 $\wedge, \vee, \neg, \dots$  classical connectives  
 $K$  modal connective

### Vocabulary:

- Syntax is classical propositional logic, plus an operator  $K$  for 'knows that'.

$$\begin{array}{c} (b \vee d)K \\ (b \vee d)K \end{array}$$

- Semantics are trickier. The idea is that an agent's beliefs can be characterized as a set of *possible worlds*, in the following way.
- Consider an agent playing a card game such as poker, who possesses the ace of spades.
- How could she deduce what cards were held by her opponents?
- First calculate all the various ways that the cards in the pack could possibly have been distributed among the various players.
- The systemically eliminate all those configurations which are not possible, given what she knows.
- (For example, any configuration in which she did not possess the ace of spades could be rejected.)

- Each configuration remaining after this is a *world*; a state of affairs considered possible, given what she knows.
- Something true in *all* our agent's possibilities is believed by the agent.
- For example, in all our agents' *epistemic alternatives*, she has the ace of spades.
- Two advantages:
  - remains neutral on the cognitive structure of agents;
  - the associated mathematical theory is very nice!

- To formalise all this, let  $W$  be a set of worlds, and let  $R \subseteq W \times W$  be a binary relation on  $W$ , characterising what worlds the agent considers possible.
- For example, if  $(w, w') \in R$ , then if the agent was actually in world  $w$ , then as far as it was concerned, it *might* be in world  $w'$ .
- Semantics of formulae are given relative to worlds: in particular:
  - $K\phi$  is true in world  $w$  iff  $\phi$  is true in all worlds  $w'$  such that  $(w, w') \in R$ .

This is *not* a desirable property!

this is *logical omniscience*.

- Thus *agents' knowledge is closed under logical consequence*:

- if  $\phi$  is valid, then  $K\phi$  is valid.

$$K(\phi \Leftarrow \psi) \Leftarrow (K\phi \Leftarrow K\psi)$$

- the following axiom schema is valid:

- Two basic properties of this definition:

$$\begin{array}{c} \text{5 } K \vdash \phi \Leftarrow K \vdash K \vdash \phi. \\ \text{4 } K \phi \Leftarrow K K \phi \\ \text{D } K \phi \Leftarrow \vdash K \vdash \phi \\ \text{T } K \phi \Leftarrow \phi \end{array}$$

- The most interesting properties of this logic turn out to be those relating to the properties we can impose on accessibility relation  $R$ . By imposing various constraints, we end up getting out various axioms; there are *lots* of these, but the most important are:

(Often chosen as a logic of *idealised belief*)

- S5 without the T is weak-S5, or KD45.

(Often chosen as a logic of *idealised knowledge*)

- All of these (KTD45) constitute the logical system S5.

want to represent our agents.

- We can (to a certain extent) pick and choose which axioms we

don't know.

- Axiom 5 is *negative introspection*: you are aware of what you

know  $\phi$ .

- Axiom 4 is *positive introspection*: if you know  $\phi$ , you know you

know  $\neg\phi$ .

- Axiom D is the *consistency axiom*: if you know  $\phi$ , you can't also

true.

- Axiom T is the *knowledge axiom*: it says that what is known is

- modal theorem proving reduces to meta-language theorem proving.
  - modal theorem proving reduces to meta-language theorem axiomatization;
  - modal formulae then translated to meta-language using first-order meta-language;
  - *but* showed how Kripke semantics could be axiomatized in a representation for action;
  - a modal logic with Kripke semantics + dynamic logic-style representation for action.
- Formal tools:
  - Moore's 1977 analysis is best-known in this area.  
*interaction between knowledge and action.*
  - Most-studied aspect of practical reasoning agents:

## 7 Knowledge & Action

- Moore considered 2 aspects of interaction between knowledge and action:
  1. As a result of performing an action, an agent can gain knowledge.
  2. In order to perform some actions, an agent needs knowledge: for example, in order to open a safe, it is necessary to know knowledge pre-conditions. For example, in order to open a safe, it is necessary to know something about the combination.
- Culminated in defn of *ability*: what it means to be able to do bring something about.

- Frege quotes,  $\llbracket \cdot \rrbracket$ , used to quote modal language formula.
- 2nd argument a term denoting modal language formula.
- 1st argument is a term denoting a world;

Here, *True* is a meta-language predicate:

$$\begin{aligned}
 & \forall w. True(w, \llbracket \phi \Rightarrow \psi \rrbracket) \Leftrightarrow (True(w, \llbracket \phi \rrbracket) \Rightarrow True(w, \llbracket \psi \rrbracket)) \\
 & \forall w. True(w, \llbracket \phi \Leftarrow \psi \rrbracket) \Leftrightarrow (\llbracket \phi \Leftarrow \psi \rrbracket \Leftrightarrow True(w, \llbracket \phi \rrbracket) \Leftarrow True(w, \llbracket \psi \rrbracket)) \\
 & \forall w. True(w, \llbracket \phi \wedge \psi \rrbracket) \Leftrightarrow True(w, \llbracket \phi \rrbracket) \wedge True(w, \llbracket \psi \rrbracket) \\
 & \forall w. True(w, \llbracket \phi \vee \psi \rrbracket) \Leftrightarrow True(w, \llbracket \phi \rrbracket) \vee True(w, \llbracket \psi \rrbracket) \\
 & \forall w. True(w, \llbracket \neg \phi \rrbracket) \Leftrightarrow (\llbracket \phi \rrbracket \rightarrow False)
 \end{aligned}$$

- Axiomatising standard logical connectives:

knowledge accessibility relation.

Here,  $K$  is a meta-language predicate used to represent the

$$\forall w \cdot \text{True}(w, \lfloor \text{Know}(\phi) \rfloor) \Leftrightarrow \forall w' \cdot K(w, w') \Leftarrow \text{True}(w', \lfloor \phi \rfloor)$$

semantics:

- Axiomatizing the knowledge connective: basic possible world

- Other axioms added to represent properties of knowledge.
    - Reflexive:
    - Transitive:
    - Euclidean:
    - These axioms ensure that  $K$  is *equivalence relation*.
- $$\forall w, w', w'' \cdot K(w, w') \vee K(w', w'') \Leftarrow K(w, w'')$$

action is  $\phi$ .

- second says that a necessary consequence of performing
- first conjunct says the action is *possible*:

$$\begin{aligned} \exists w' \cdot R(a, w, w') \vee \exists w'' \cdot R(a, w, w'') \Leftarrow \text{True}(w'', \lfloor \phi \rfloor) \\ \forall w. \text{True}(w, \lfloor (\text{Res } a \phi) \rfloor) \Leftrightarrow \end{aligned}$$

*action a is performed,  $\phi$  will be true.*

- Then introduce a modal operator ( $\text{Res } a \phi$ ) to mean that *after* world that could result from performing action  $a$  in world  $w$ .
- Add a meta-language predicate  $R(a, w, w')$  to mean that  $w'$  is a world that could result from performing action  $a$  in world  $w$ .
- Now we need some apparatus for representing *actions*.

(Terminology:  $a$  is quantified *de re*)

Has a "definite description" of it.

Implies agent knows the identity of the action.

- Note the way  $a$  is quantified w.r.t. the know modality.

agent knows that the result of performing  $a$  is  $\phi$ .

So agent can achieve  $\phi$  if there exists some action  $a$ , such that

$$\begin{aligned} \exists a. \text{True}(w, \lfloor (\text{Know } (\text{Res } a \phi)) \rfloor) \\ \forall w. \text{True}(w, \lfloor (\text{Can } \phi) \rfloor) \Leftrightarrow \end{aligned}$$

- Now we can define ability, via modal Can operator.

- We can weaken the definition, to capture the case where an agent performs an action to find out how to achieve goal.

$$\begin{aligned} \exists w \cdot \text{True}(w, \lfloor (\text{Can } \phi) \rfloor) &\Leftrightarrow \\ \exists w \cdot \text{True}(w, \lfloor (\text{Know } (\text{Res } a \phi)) \rfloor) \vee \\ \exists a \cdot \text{True}(w, \lfloor (\text{Know } (\text{Res } a (\text{Can } \phi))) \rfloor) \end{aligned}$$

A circular definition?

No, interpret as a *fixed point*.

- Critique of Moore's formalism:
  1. Translating modal language into a first-order one and then theorem proving in first-order language is inefficient.  
“Hard-wired” modal theorem provers will be more efficient.
  2. Formulate resulting from the translation process are complicated and unintuitive.
  3. Moore's formalism based on possible worlds: fails prey to original structure (and hence sense) is lost.
- But probably first serious attempt to use tools of mathematical logic (incl. modal & dynamic logic) to bear on rational agency.

It is my intention to prepare my slides.

- Here we mean intention as in . . .  
the theory of intention developed by Cohen & Levesque.  
how the components of an agent's cognitive state hold together:
- Here, we review one attempt to produce a coherent account of
  - should not be *under-committed*.
  - should not be *over-committed*.
- Agent needs to achieve a *rational balance* between its attitudes:  
*pro-attitudes* as well.
- We need a *set* of connectives, for talking about an agent's  
does not completely characterise an agents.
- We have *one aspect* of an agent, but knowledge/belief alone

## 8 Intention

- We are here concerned with *future directed* intentions.
  - \* serve to coordinate future activity.
  - \* attitude to a proposal
    - *future directed*
  - \* function causally in producing behaviour.
  - \* attitude to an action
    - *present directed*
- Two sorts:

## 8.1 What is intention?

- Following Bratman (1987) Cohen-Levesque identify seven properties that must be satisfied by intention:
1. Intentions pose problems for agents, who need to determine ways of achieving them.
  2. Intentions provide a ‘filter’ for adopting other intentions, which must not conflict.  
*If I have an intention to  $\phi$ , you would expect me to devote resources to deciding how to bring about  $\phi$ .*
  3. Agents track the success of their intentions, and are inclined to try again if their attempts fail.  
*If an agent’s first attempt to achieve  $\phi$  fails, then all other things being equal, it will try an alternative plan to achieve  $\phi$ .*

In addition . . .

- Agents believe their intentions are possible.

That is, they believe there is at least some way that the intentions could be brought about. ( $CTL^*$  notation:  $E\Diamond\phi$ ).
- Agents believe their intentions are possible.

Agents do not believe they will not bring about their intentions.
- It would not be rational of me to adopt an intention to  $\phi$  if I believed  $\phi$  was not possible. ( $CTL^*$  notation:  $A\Box\neg\phi$ .)

It would not be rational of me to adopt an intention to  $\phi$  if I believed  $\phi$  was not possible. ( $CTL^*$  notation:  $A\Box\neg\phi$ .)

- Under certain circumstances, agents believe they will bring about their intentions.
- Under certain circumstances, agents believe they will bring about it would not normally be rational of me to believe that I would bring my intentions about; intentions can fail. Moreover, it does not make sense that if I believe  $\phi$  is inevitable (CTL\*:  $A\Diamond\phi$ ) that I would adopt it as an intention.
- Agents need not intend all the expected side effects of their intentions.
  - If I believe  $\phi \Leftarrow \psi$  and I intend that  $\psi$ , I do not necessarily intend  $\psi$  also. (Intentions are not closed under implication.)
  - This last problem is known as the **dentist** problem. I may believe that going to the dentist involves pain, and I may also intend to go to the dentist — but this does not imply that I intend to suffer pain!

- Cohen-Levesque use a **multi-modal logic** with the following major constructs:
  - (Bel  $x \phi$ )  $x$  believes  $\phi$
  - (Goal  $x \phi$ )  $x$  has goal of  $\phi$
  - (Happens  $a$ ) action  $a$  happens next
  - (Done  $a$ ) action  $a$  has just happened
  - Each world is infinitely long linear sequence of states.
  - Each agent allocated:
  - Euclidean, serial, transitive — gives belief logic KD45.
  - for every agent/time pair, gives a set of belief accessible worlds;
  - belief accessibility relation** —  $B$

- **goal accessibility relation** —  $G$
- for every agent/time pair, gives a set of goal accessible worlds.
- Serial — gives goal logic KD.

- agents do not indefinitely defer working on goals.
- agents do not persist with goals forever;

C<sub>8</sub>L claim this assumption captures following properties:

$$\models (\text{Goal} \ i \ \phi) \Leftarrow \Diamond \Box (\text{Goal} \ i \ \phi)$$

- Another constraint:

- A *realism* property — agents *accept the inevitable*.

$$\models (\text{Bel} \ i \ \phi) \Leftarrow (\text{Goal} \ i \ \phi)$$

- Gives the following inter-modal validity:

- A constraint:  $G \bar{\sqsubset} B$ .

- Add in some operators for describing the structure of event sequences
  - $a? \text{ test action } a$
  - $a; a \text{ followed by } a'$
- Also add some operators of temporal logic, “ $\Box$ ” (always), and “ $\Diamond$ ” (sometime) can be defined as abbreviations, along with a “ $\Diamond$ ” (sometime operator, Later:
  - $\Diamond a = \exists x \cdot (\text{Happens } x; a?)$
  - $\Box a = \forall x \Diamond \neg a$
  - $(\text{Later } p) = \exists d \Box (p \vee \Diamond d)$

hold:

2. Before it drops the goal, one of the following conditions must

that  $p$  is not currently true.

1. It has a goal that  $p$  eventually becomes true, and believes

- So, an agent has a persistent goal of  $p$  if:

$$\begin{aligned}
 & \neg(\text{Goal } x (\text{Later } p)) \\
 & \neg(\text{Bel } x p) \vee (\text{Bel } x \Box \neg p) \\
 & \neg(\text{Bel } x \neg p) \\
 & \neg(\text{Goal } x (\text{Later } p)) \\
 & \neg(\text{P} - \text{Goal } x p) = 
 \end{aligned}$$

- First major derived construct is a **persistent** goal.
- Finally, a temporal precedence operator,  $(\text{Before } p \ q)$ .

- the agent believes the goal has been satisfied;
- the agent believes the goal will never be satisfied.

- Adaptation of definition allows for **relativised intentions**. Example:
    - Main point: avoids **ever commitment**.
    - CGL discusses how this definition satisfies desiderata for intention.
    - So, an agent has an intention to do  $a$  if: it has a persistent goal to have believed it was about to do  $a$ , and then done  $a$ .
- will not be paid, the intention evaporates. . .  
belief that I will be paid for tutorial. If I ever come to believe that I have an intention to prepare slides for the tutorial, **relative** to the belief that I will be paid for tutorial. If I ever come to believe that I will not be paid, the intention evaporates. . .

$$\begin{aligned}
 (\text{Intend } x \ a) &= \\
 (\text{P-Goal } x) &\\
 [\text{Done } x \ (\text{Bel } x \ (\text{Happens } a))?) ; a] &
 \end{aligned}$$

- Next, intentions:

- Critique of C&L theory of intention (Singh, 1992):
  - does not capture and adequately represent notion of "competence";
  - does not adequately represent intentions to do composite actions;
  - requires that agents know what they are about to do — fully elaborated intentions;
  - disallows multiple intentions.

$$\begin{aligned}
 & \text{(AltBel } n \ x \ y \ p) \underset{\text{n times}}{=} \\
 & \quad \overbrace{(\text{Bel } x \ (\text{Bel } y \ (\text{Bel } x \cdots (\text{Bel } x \ p \ ) \cdots))}^{\text{n times}}
 \end{aligned}$$

- First, define *alternating belief*.
- We will look at *request*.
- CGL used their dynamic logic-style formalism for representing these actions.
- CGL used their theory of intention to develop a theory of several speech acts.
- Key observation: illocutionary acts are *complex event types* (cf. actions).
- We will look at *requests*.

## 9 Semantics for Speech Acts

- And the related concept of *mutual belief*.

$$(M - Bel(x \wedge d)) \stackrel{?}{=} An \cdot (AltBel(n \wedge x \wedge d))$$

- $p$  represents ultimate goal that agent is aiming for by doing  $e$ :

Here:

“An attempt is a complex action that agents perform when they do something  $(e)$  desiring to bring about some effect  $(d)$  but with intent to produce at least some result  $(y)$ ”.

In English:

$$\{\text{Attempt } x \in p \mid y\} = \begin{cases} (\text{Intent } x \in e; d) \\ (\text{Goal } x \text{ Happens } x \in e; d) \\ (\text{Bel } x \vdash d) \end{cases}$$

- An **attempt** is defined as a complex action expression.  
 (Hence the use of curly brackets, to distinguish from predicate or modal operator.)

- **proposal** represents what it takes to at least make an “honest effort” to achieve  $p$ .

“[C]onsider an agent [ $x$ ] to be helpful to another agent [ $y$ ] if, for any action [ $e$ ] he adopts the other agent’s goal that he eventually do that action, whenever such a goal would not conflict with his own”.

In English:

$$(Helpful xy) \equiv A_e . \left[ \begin{array}{l} (\text{Bel } x (\text{Goal } y \diamond (\text{Done } xe))) \vee \\ \neg (\text{Goal } x \Box \neg (\text{Done } xe)) \end{array} \right] \Leftarrow (\text{Goal } x \diamond (\text{Done } xe))$$

- Definition of *helpfulness* needed:

In English:

$$\begin{array}{c}
 (\text{Helpful addr spkr}) \\
 [(\text{Goal spkr} \diamond (\text{Done addr } a)) \vee \\
 (\text{Intend addr } a) \\
 \diamond (\text{Done addr } a)] \vee \\
 [(\text{Goal spkr} \diamond (\text{Done addr } a)) \vee
 \end{array}$$

where  $\phi$  is

$$\begin{array}{c}
 \{ \\
 (\text{M - Bel addr spkr} (\text{Goal spkr } \phi)) \\
 \{ \text{Attempt spkr } e \in \phi \\
 \{ \text{Request spkr addr } e \in a \} \subseteq
 \end{array}$$

- Definition of *requests*:

A request is an attempt on the part of *spkr*, by doing *e*, to bring about a state where, ideally, 1) *addr* intends a, bringing about a state where, ideally, 1) *addr* intends a, (relative to the *spkr* still having that goal, and *addr* still being helpfully inclined to *spkr*), and 2) *addr* actually eventually does a, or at least brings about a state where *addr* believes it is mutually believed that it wants the ideal situation.

- By this definition, there is no primitive request act:  
“[A] speaker is viewed as having performed a request if he executes any sequence of actions that produces the needed effects”.

- We now move on to a theory of **cooperation** (or more precisely, cooperative problem solving). This theory draws on work such as CGIL's model of intention, and it uses connectives such as 'intend' as the building blocks.
- It uses semantics for speech acts. The theory intends to explain how an agent can start with an desire, and be moved to get other agents involved with achieving this desire.

## 10 A Theory of Cooperation

- We formalise our theory by expressing it in a quantified multi-modal logic.
- Formal semantics in the paper:
  - with agents.
  - actions (transitions in branching time structure) associated theoretic mechanism for reasoning about groups;
  - groups (sets of agents) as terms in the language — set
  - path quantifiers (branching time);
  - dynamic logic style action constructors;
  - goals;
  - beliefs;

## 11 A(nother) Formal Framework

## 12 The Four-Stage Model

1. **Recognition.**  
CPS begins when some agent recognises the potential for cooperative action.  
May happen because an agent has a goal that it is unable to achieve in isolation, or because the agent prefers assistance.
2. **Team formation.**  
The agent that recognised the potential for cooperative action at stage (1) solicits assistance.  
If team formation successful, then it will end with a group having a joint commitment to collective action.

http://www.csc.liv.ac.uk/~mjw/pubs/images/50

### 3. Plan formation.

The agents attempt to negotiate a joint plan that they believe will achieve the desired goal.

### 4. Team action.

The newly agreed plan of joint action is executed by the agents, which maintain a close-knit relationship throughout.

- CPs typically begins when some agent in a has a goal, and recognises the potential for cooperative action with respect to that goal.
- Recognition may occur for several reasons:
  - The agent is unable to achieve its goal in isolation, due to a lack of resources, but believes that cooperative action can achieve it.
  - An agent may have the resources to achieve the goal, but does not want to use them.
  - It may believe that in working alone on this particular problem, it will clobber one of its other goals, or it may believe that a cooperative solution will in some way be better.

## 12.1 Recognition

- Doesn't mean it doesn't happen next.

- (Achieves  $a \phi$ ) is dynamic logic  $[a]\phi$ :

- J - Can is a generalization of Moore's

- Can is essentially Moore's;

- Note:

$$\text{Potential-for-Coop } i \phi = \text{Goal } i \phi \vee
 \begin{bmatrix}
 \neg(\text{Can } i \phi) \vee \\
 (\text{Bel } i Aa \cdot (\text{Agt } a i)) \vee \\
 (\text{Achieves } a \phi) \Leftarrow \\
 (\text{Goal } i (\text{Doesn't } a))
 \end{bmatrix}$$

- Formally...

- Having identified the potential for cooperative action with respect to one of its goals, a rational agent will solicit assistance from some group of agents that it believes can achieve the goal.
- If the agent is successful, then it will have brought about a mental state wherein the group has a joint commitment to collective action.
- Note that agent cannot guarantee that it will be successful in forming a team, it can only *attempt* it.

## 12.2 Team Formation

## • Formally . . .

## • Note that:

$$\begin{aligned} & (\text{J - Commit } g (\text{Team } g \phi_i) (\text{Goal } i \phi) \dots) \\ & (\text{M - Bel } g (\text{J - Can } g \phi)) \vee \\ & (\text{PreTeam } g \phi_i) \end{aligned}$$

- J - Commit is similar to J - P - Goal.
- Team is defined in later;

$$\begin{aligned} q &= (\text{M} - \text{Bel } g(\text{Goal } i \phi) \vee (\text{Bel } i(\text{J} - \text{Can } g \phi))). \\ p &= (\text{PreTeam } g \phi i) \end{aligned}$$

where

$$\begin{aligned} &\forall \exists g \cdot \exists a \cdot (\text{Happens } \{\text{Attempt } i a p\} g) \\ &\Leftarrow \forall i \cdot (\text{Bel } i (\text{Potential-for-Coop } i \phi)) \end{aligned}$$

stated.

- The main assumption concerning team formation can now be

- Unfortunately, negotiation is extremely complex — we simply offer some observations about the weakest conditions under which negotiation can be said to have occurred.
- Hence the next stage in the CPS process: plan formation, which involves *negotiation*.
- But collective action cannot begin until the group agree on what they will actually do.
- If team formation is successful, then there will be a group of agents with a joint commitment to collective action.
- Hence the next stage in the CPS process: plan formation, which involves *negotiation*.

## 12.3 Plan Formation

- If negotiation succeeds, we expect a team action stage to follow.
  - say that negotiation occurred at all is that *at least one* agent proposed a course of action that it believed would take the collective closer to the goal.
- In this case, the minimum condition required for us to be able to
  - Note that negotiation may *fail*: the collective may simply be unable to reach agreement.

$$\begin{aligned}
 & \cdot (\text{Gets } a \ g) \vee (\text{Achieves } a \ \phi)). \\
 & (\text{M} - \text{Bel } g \ (\text{Bel } j) \\
 & \quad \vee \exists j \cdot \exists a \cdot (j \in g \ \forall b \ \\
 & \quad \quad \quad (\text{M} - \text{Know } g \ (\text{Team } g \ \phi \ i))
 \end{aligned}$$

where

$$\begin{aligned}
 & \text{A}^\diamond \exists a \cdot (\text{Happens } j - \text{Attempt } g \ a \ d \ y) \\
 & \Leftarrow (\text{PreTeam } g \ \phi \ i)
 \end{aligned}$$

- The main assumption is then:  
For example, if an agent has an objection to some plan, then it will attempt to prevent this plan being carried out.
- We might also assume that agents will attempt to bring about their preferences.

$$(\exists i \text{ - Intend } g_a (\text{Goal } i \phi)) \vee \\ (\text{Team } g \phi i) \equiv \exists a \cdot (\text{Achieves } a \phi) \vee$$

- The formalisation of Team is simple.
- Team action simply involves the team jointly intending to achieve the goal.

## 12.4 Team Action