cc3.12/cis1.0 computing: nature, power and limits—robotics applications fall 2007 lecture # III.1 data representation and storage • data representation • file storage • speed of data transmission resources: • reading: Reed chapter 12 and 14	 data representation: bits a bit is the smallest unit of memory bit = binary digit a bit is a <i>switch</i> inside the computer; the setting (or value) of each switch is either ON (= 1) or OFF (-0) all data in a computer is represented by <i>bit patterns</i>, i.e., sequences of 0's and 1's all numbers can be represented by 0's and 1's in <i>base 2</i> hence the term <i>binary</i> computer!
cc3.12-fall2007-sklar-lecili.1 1 data representation: bytes	cc3.12-fall2007-sklar-lecl11.1 2 data representation: base 2
• a byte is a sequence of 8 bits • thus there are $2^8 = 256$ possible values that can be represented by one byte • values range from 0 to $2^8 - 1 = 256 - 1 = 255$ • where $0 = 00000000$ and $255 = 1111111$	 in base 2, only the digits 0 and 1 are used just like base 10, each digit, from the right to the left, indicates how many of each base raised to a power are contained in the number that is represented probably an example will help: note that digits are counted from right to left, starting with 0 to convert a byte to base 10, multiply each digit in the byte by the value in the table below, then add them all together so, to convert 00001011, look up each digit in the table above, and you get this:
cc3.12-fall2007-sklar-lecIII.1 3	cc3.12-fall2007-sklar-lecll1.1 4

ugit: 1 0 5 4 5 2 1 0 power: 2^7 2^6 2^5 2^4 2^3 2^2 2^1 2^0 value: 128 64 32 16 8 4 2 1 × byte: 0 0 0 1 0 1 1 = 0 × 128 0 × 64 0 × 32 0 × 16 1 × 8 0 × 4 1 × 2 1 × 1 = 0 + 0 + 0 + 0 + 8 + 0 + 2 + 1 = 11 (in base 10) 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 <th>power: 2^7 2^6 2^5 2^4 2^3 2^2 2^1 2^0 value: 128 64 32 16 8 4 2 1 × byte: 0 0 0 1 0 1 1 = 0 × 128 0 × 64 0 × 32 0 × 16 1 × 8 0 × 4 1 × 2 1 × 1 = 0 + 0 + 0 + 2 + 1</th> <th></th> <th>7</th> <th>6</th> <th>5</th> <th>4</th> <th>3</th> <th>2</th> <th>1</th> <th>0</th>	power: 2^7 2^6 2^5 2^4 2^3 2^2 2^1 2^0 value: 128 64 32 16 8 4 2 1 × byte: 0 0 0 1 0 1 1 = 0 × 128 0 × 64 0 × 32 0 × 16 1 × 8 0 × 4 1 × 2 1 × 1 = 0 + 0 + 0 + 2 + 1		7	6	5	4	3	2	1	0
value: 128 64 32 16 8 4 2 1 × byte: 0 0 0 1 0 1 1 = 0 × 128 0 × 64 0 × 32 0 × 16 1 × 8 0 × 4 1 × 2 1 × 1 = 0 + 0 + 0 + 8 + 0 + 2 + 1	value: 128 64 32 16 8 4 2 1 × byte: 0 0 0 1 0 1 1 = 0 × 128 0 × 64 0 × 32 0 × 16 1 × 8 0 × 4 1 × 2 1 × 1 = 0 + 0 + 0 + 8 + 0 + 2 + 1	digit:								
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$									
= 0 + 0 + 0 + 0 + 8 + 0 + 2 + 1	= 0 + 0 + 0 + 0 + 8 + 0 + 2 + 1	\times byte:	0	0	0	0	1	0	1	1
		=	0×128	0×64	0×32	0×16	1×8	0×4	1×2	1×1
= 11 (in base 10)	= 11 (in base 10)	=			+ 0	+ 0	+ 8	+ 0	+ 2	+ 1
		=	11 (in ba	ise 10)						

	base 2	base 8	base 16
0	0	0	0
1	1	1	1
2	10	2	2
3	11	3	3
4	100	4	4
5	101	5	5
6	110	6	6
7	111	7	7
8	1000	10	8
9	1001	11	9
10	1010	12	A
11	1011	13	В
12	1100	14	C
13	1101	15	D
14	1110	16	E
	1111	17	F

data representation: other bases base 8, or octal since 2³ = 8, it is often convenient to compress 3-digit binary values as base 8, or octal values base 16, or hexadecimal since 2⁴ = 16, it is often convenient to compress 4-digit binary values as base 16, or hexadecimal values it is handy to memorize (or at least, to know how to derive) the following table of base 2, 8 and 16 numbers from 0 to 15:

exercise convert 13_{base8} to base 10: 13_8 $= (1 \times 8^1) + (3 \times 8^0)$ $= (1 \times 8) + (3 \times 1)$ = 8 + 3= 11

data storage: storing numbers in a computer

- now you know the basis for how numbers are stored
- \bullet but all numbers are not just values between 0 and 255
- some are very large, some are real (i.e., have decimal points), some are negative
- negative numbers are represented using something called two's complement notation in which the leftmost bit is a sign bit and some operations are performed on the digits in order to determine the value of the negative number; we will not go into this level of detail...
- real numbers are represented using something called **floating point notation** in which the whole and fractional parts of the number are stored separately and some operations are performed on the digits in order to put the pieces together and determine the value of the real number;

we will not go into this level of detail...

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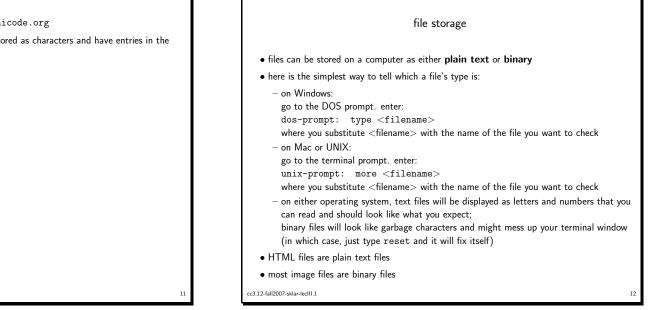
• for more information, go to http://www.unicode.org

• NOTE that the digits 0, 1, 2, ..., 9 can be stored as characters and have entries in the ASCII and Unicode tables

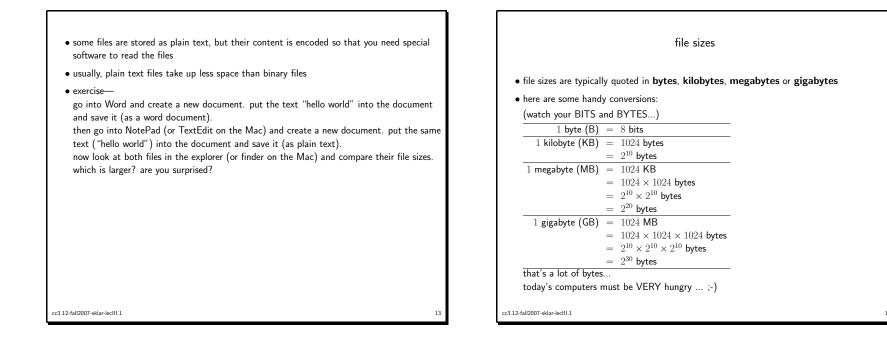
data storage: storing letters in a computer

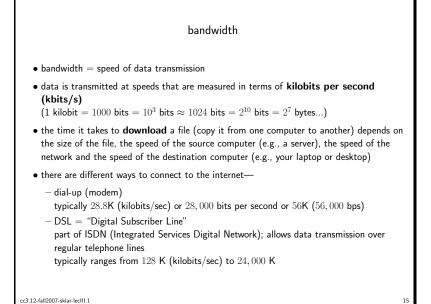
- letters, or *characters*, are stored as numbers, but are encoded so that for each character on the keyboard (or displayed on the screen) there is a (positive) number that represents that character
- the software reading the value has to know that it should be interpreted as a character rather than a number
- the standard encoding is called **ASCII** (American Standard Code for Information Interchange)
- standard ASCII encodes 128 characters
- extended ASCII encodes 128 more, to total 256 characters
- Unicode uses 2 bytes and encodes $2^{16} = 65536$ characters (!) in many languages
 - "Unicode provides a unique number for every character, no matter what the platform,
 - no matter what the program, no matter what the language."
 - (from http://www.unicode.org)

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cc3.12-fall2007-sklar-lecIII.1





cable modem

carries data transmissions over digital cable television lines typically ranges from $384~{\rm K}$ (kilobits/sec) to $30~{\rm M}$ (megabits/sec) for a fast business line

exercise—

take the $\ensuremath{\textbf{speakeasy}}$ speed test:



http://www.speakeasy.net/speedtest/

cc3.12-fall2007-sklar-lecIII.1