cis32-ai — lecture # 5 — wed-15-feb-2006

today's topics:

• heuristic search (part 1 of 2)

Recap

The last lecture introduced

- Basic problem solving techniques:
 - Breadth-first search
 - Depth-first search
- Breadth-first search is complete but expensive.
- Depth-first search is cheap but incomplete
- Can't we do better than this?
- That is what this lecture is about

Overview

Aims of this lecture:

- show how basic search (depth 1st, breadth 1st) can be improved;
- introduce:
 - depth limited search;
 - iterative deepening.
- show that even with such improvements, search is hopelessly unrealistic for real problems.

Algorithmic Improvements

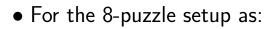
- Are then any *algorithmic* improvements we can make to basic search algorithms that will improve overall performance?
- Try to get *optimality* and *completeness* of breadth 1st search with *space efficiency* of depth 1st.
- Not too much to be done about time complexity :-(

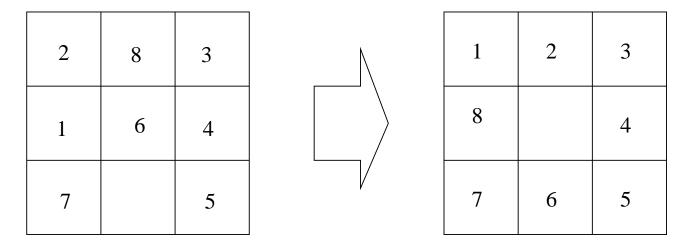
Depth Limited Search

- Depth first search has some desirable properties space complexity.
- But if wrong branch expanded (with no solution on it), then it won't terminate.
- Idea: introduce a *depth limit* on branches to be expanded.
- Don't expand a branch below this depth.

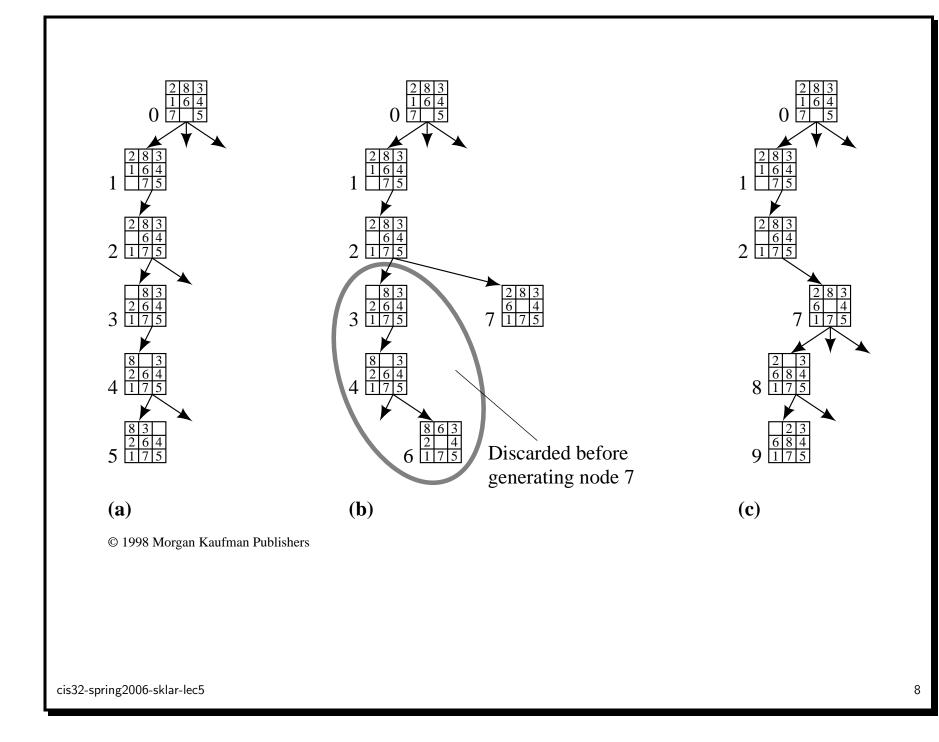
• General algorithm for depth limited search:

```
depth limit = max depth to search to;
   agenda = initial state;
   while agenda not empty do
     take node from front of agenda;
     new nodes = apply operations to node;
     if goal state in new nodes then {
       return solution;
     }
     if depth(node) < depth limit then {</pre>
       add new nodes to front of agenda;
     }
   }
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```





• the search will be as follows:



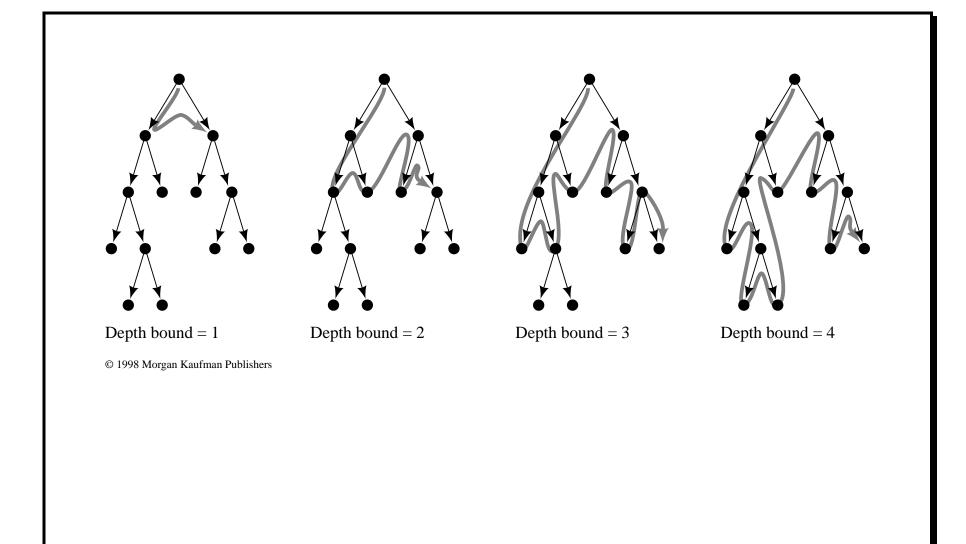
- So, when we hit the depth bound, we don't add any more nodes to the agenda.
- Then we pick the next node off the agenda.
- This has the effect of moving the search back to the last node above depth limit that that is "partly expanded".
- This is known as *chronological backtracking*.
- The effect of the depth limit is to force the search of the whole state space down to the limit.
- We get the completeness of breadth-first (down to the limit), with the space cost of depth first.

Iterative Deepening

- Unfortunately, if we choose a max depth for d.l.s. such that shortest solution is longer, d.l.s. is not complete.
- Iterative deepening an ingenious *complete* version of it.
- Basic idea is:
 - do d.l.s. for depth 1; if solution found, return it;
 - otherwise do d.l.s. for depth n; if solution found, return it;
 - otherwise,
- So we *repeat* d.l.s. for all depths until solution found.

• General algorithm for depth limited search:

```
depth limit = 1;
repeat {
  result = depth_limited_search(
    max depth = depth limit;
    agenda = initial node;
  );
  if result contains goal then {
    return result;
  }
  depth limit = depth limit + 1;
  } until false; /* i.e., forever */
• Calls d.l.s. as subroutine.
```



- Note that in iterative deepening, we *re-generate nodes on the fly.* Each time we do call on depth limited search for depth d, we need to regenerate the tree to depth d - 1.
- Isn't this inefficient?
- Tradeoff *time* for *memory*.
- In general we might take a *little* more time, but we save a *lot* of memory.
- Now for breadth-first search to level *d*:

$$N_{bf} = 1 + b + b^{2} + b$$
$$= \frac{b^{d+1} - 1}{b - 1}$$

• In contrast a complete depth-limited search to level j:

$$N_{df}^{j} = \frac{b^{j+1} - 1}{b - 1}$$

- (This is just a breadth-first search to depth *j*.)
- \bullet In the worst case, then we have to do this to depth d, so expanding:

$$N_{id} = \sum_{j=0}^{d} \frac{b^{j+1} - 1}{b - 1}$$

:
$$= \frac{b^{d+2} - 2b - bd + d + 2}{(b - 1)^2}$$

• For large *d*:

$$\frac{N_{id}}{N_{bf}} = \frac{b}{b-1}$$

• So for high branching and relatively deep goals we do a small amount more work.

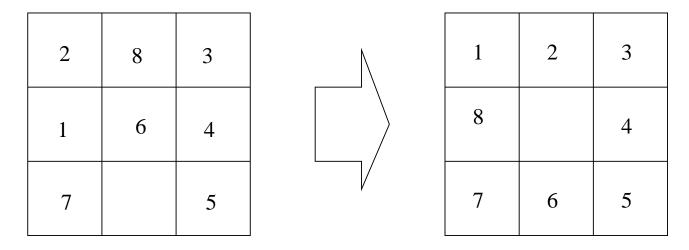
• Example: Suppose b = 10 and d = 5.

Breadth first search would require examining 111, 111 nodes, with memory requirement of 100,000 nodes.

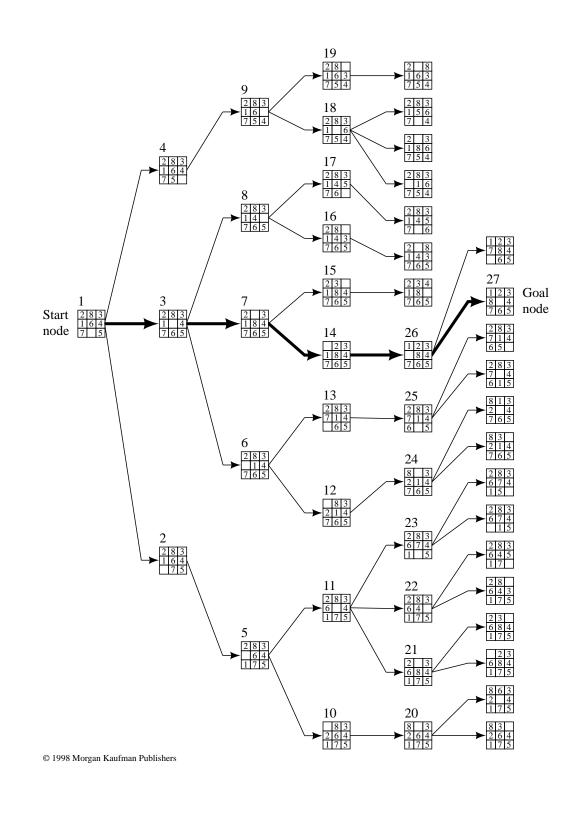
Iterative deepening for same problem: 123,456 nodes to be searched, with memory requirement only 50 nodes.

Takes 11% longer in this case.

• For the 8-puzzle setup as:



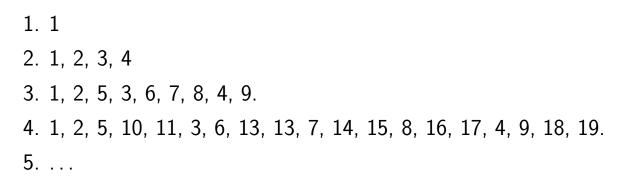
- What would iterative deepening search look like?
- Well, it would explore the search space:



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- In the following way.
- States would be expanded in the order:



• Note that these are the states *visited*, not the nodes on the agenda.

Bi-directional Search

- Suppose we search from *the goal state backwards* as well as from *initial state forwards*.
- Involves determining *predecessor* nodes to goal, and then looking at predecessor nodes to this, ...
- Rather than doing one search of b^d , we do *two* $b^{d/2}$ searches.
- *Much* more efficient.

• Example:

Suppose b = 10, d = 6.

Breadth first search will examine nodes.

Bidirectional search will examine nodes.

- Can combine different search strategies in different directions.
- For large *d*, is still impractical!

Summary

- This lecture has looked at some more efficient techniques than breadth first and depth first search.
 - depth-limited search;
 - iterative-deepening search; and
 - bidirectional search.
- These all improve on depth-first and breadth-first search.
- However, all fail for big enough problems (too large state space).
- Next lecture, we will look at approaches that cut down the size of the state-space that is searched.