

Discrete Structures - Test 1 (Sample)

12:50-2:05, Oct 13, 2010 (Wednesday)

Name:_____

Answer all six questions.

Question 1 [4 points]

Let $A = \{1, 2, 3, 4, 5, 6, 7\}$. Give each of the following sets.

1. $B = \{n \in A : n \text{ is odd}\}$
2. $C = \{n + 4 : n \in A\}$
3. $D = B \cup C$
4. $E = B \cap C$
5. $F = B \setminus C$
6. $G = B \oplus C$
7. $P(E)$ - the power set of E
8. $E \times E$ - the Cartesian product of E and E

Question 2 [3 points]

Use Venn diagrams to prove the De Morgan law $(A \cap B)^c = A^c \cup B^c$.

Question 3 [3 points]

Consider the function $f(x)=2x+3$ from Z to Z .

1. Is f one-to-one?
2. Is f onto Z ?
3. Is f invertible? If so, what is the inverse function?
4. What is $f \circ f$?

Question 4 [3 points]

Build the truth tables for $(\neg p \vee \neg q)$ and $\neg(p \wedge q)$.

Question 5 [3 points]

Prove that the sum of three consecutive integers is divisible by 3.

Question 6 [4 points]

Here is a proof by contradiction for the following theorem: If $p \vee (q \rightarrow r)$, $q \vee r$, and $r \rightarrow p$, then p . For each step, supply an explanation.

1. $p \vee (q \rightarrow r)$
2. $q \vee r$
3. $r \rightarrow p$
4. $\neg p$
5. $\neg r$
6. $r \vee q$
7. q
8. $q \rightarrow r$
9. r
10. $r \wedge \neg r$
11. contradiction