

Homework

Recursion

Question 1

Consider the following TowerOfHanoi program:

```
public class TowerOfHanoi {
    public static void main(String[] args) {
        moveDisks(3, 'A', 'B', 'C');
    }

    /** The method for finding the solution to move n disks
        from fromTower to toTower with auxTower */
    public static void moveDisks(int n, char fromTower, char toTower, char auxTower) {
        if (n == 1) // Stopping condition
            System.out.println("Move disk " + n + " from " +
                               fromTower + " to " + toTower);
        else {
            moveDisks(n - 1, fromTower, auxTower, toTower);
            System.out.println("Move disk " + n + " from " +
                               fromTower + " to " + toTower);
            moveDisks(n - 1, auxTower, toTower, fromTower);
        }
    }
}
```

1. How many times is the function `moveDisks` invoked?
2. Sketch what calls are on the run-time stack right after the message “Move disk 1 from C to A” is printed out.

Question 2

Implement each of the following functions using *recursion* in Java.

1. `static int sum_of_squares(int n)`: Return the summation of squares $\sum_{k=1}^n (k^2)$.
2. `static int gcd(int x, int y)`: Return the greatest common divisor of `x` and `y`.
3. `static int sumEven(int[] a)`: Return the sum of the even integers in array `a`.
4. `static boolean sorted(int[] a)`: Test if array `a` is sorted in ascending order.
5. `static int[] copy(int[] a)`: Return a copy of array `a`.
6. `public static int count(String str, char a)`: Return the number of occurrences of character `a` in string `str`.
7. `static long bin_str_to_int(String binStr)`: Convert an unsigned binary string to a decimal integer. For example, for `binStr = 11010`, the returned integer is 26.